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## The Product of a Compactum with a Polyhedron in the Shape Categories

In the ordinary shape category  $\text{Sh}(\text{Top})$ , as well as in the strong shape category  $\text{SSh}(\text{Top})$ , the Cartesian product of two polyhedra, together with the canonical projections, is their categorical product. The analogous assertion holds for the Cartesian product of two compact Hausdorff spaces.

**PROBLEM.** *Let  $X$  be a compact Hausdorff space and let  $P$  be a polyhedron. Is  $X \times P$ , together with the canonical projections  $\Pi_X: X \times P \rightarrow X$  and  $\Pi_P: X \times P \rightarrow P$ , the categorical product of  $X$  and  $P$  in  $\text{Sh}(\text{Top})$  and  $\text{SSh}(\text{Top})$ ?*

The author hopes to solve this problem using a particular resolution  $\mathbf{q}: X \times P \rightarrow \mathbf{Y} = (Y_\mu, q_{\mu\mu'}, M)$ , induced by a polyhedral resolution  $\mathbf{p}: X \rightarrow \mathbf{X} = (X_\lambda, p_{\lambda\lambda'}, \Lambda)$  and by a triangulation  $K$  of  $P$ . The index set  $M$  consists of all increasing functions  $\mu: K \rightarrow \Lambda$ , where  $K$  is ordered by putting  $\sigma \leq \sigma'$ , provided  $\sigma$  is a face of  $\sigma'$ .  $Y_\mu = \tilde{Y}_\mu / \sim_\mu$ , where  $\tilde{Y}_\mu$  is the disjoint sum of all products  $X_{\mu(\sigma)} \times \sigma$ ,  $\sigma \in K$ , and  $(x, t) \sim_\mu (x', t')$  if  $(x, t) \in X_{\mu(\sigma)} \times \sigma$ ,  $(x', t') \in X_{\mu(\sigma')} \times \sigma'$ ,  $\sigma \leq \sigma'$ ,  $p_{\mu(\sigma)\mu(\sigma')}(x') = x$  and  $i_{\sigma\sigma'}(t) = t'$ ; here  $i_{\sigma\sigma'}: \sigma \rightarrow \sigma'$  is the inclusion mapping.

**THEOREM.** *Let  $X$  be a metric compactum and let  $P$  be a separable polyhedron. Then for every topological space  $Z$  and strong shape morphisms  $F: Z \rightarrow X$ ,  $G: Z \rightarrow P$ , there exists a strong shape morphism  $H: Z \rightarrow X \times P$  such that  $\Pi_X H = F$  and  $\Pi_P H = G$ .*

To solve affirmatively the above stated problem for  $\text{SSh}(\text{Top})$ , compact metric  $X$  and separable polyhedra  $P$ , it remains to prove uniqueness of  $H$ .

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