

The background image is a photograph of a waterfall in a lush, green forest. The water flows over moss-covered rocks, creating a misty spray. The surrounding trees are dense and vibrant green, with sunlight filtering through the canopy. A small pool of water is visible at the base of the falls.

2.10. Prirodna domena

27.10.2020.

Zadatak 20

Odredite prirodnu domenu funkcije

$$f(x) := \frac{\ln(x^2)}{\sqrt{\arcsin(1-x^2)}}. \quad (1)$$

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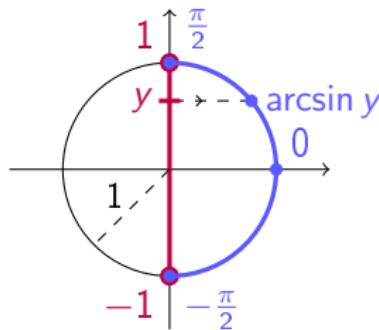
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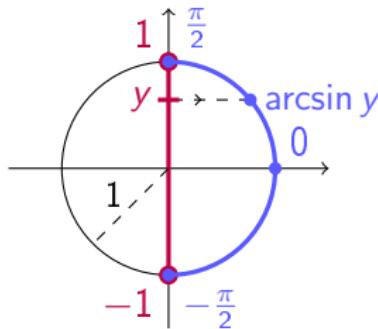
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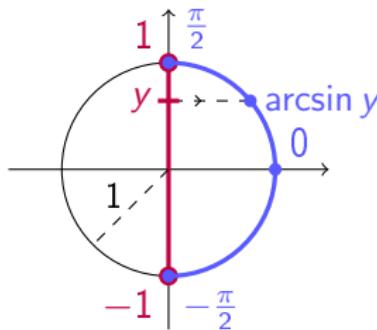
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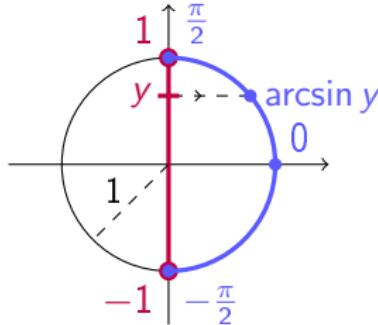
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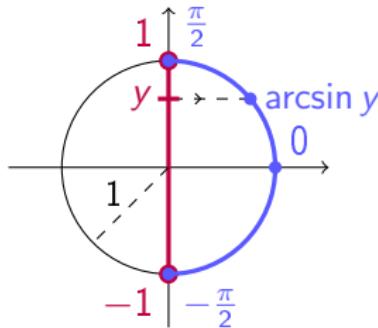
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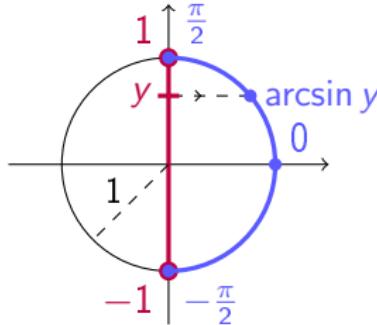
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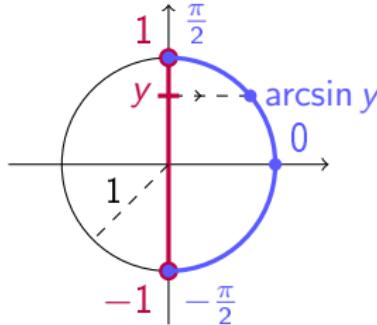
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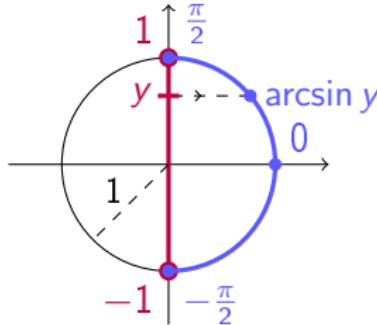
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