

$f(x)$	$\mathcal{L}(f)(s)$
δ_0	1
1	$\frac{1}{s}$
x	$\frac{1}{s^2}$
x^n	$\frac{n!}{s^{n+1}}$
e^{ax}	$\frac{1}{s-a}$
xe^{ax}	$\frac{1}{(s-a)^2}$
$x^n e^{ax}$	$\frac{n!}{(s-a)^{n+1}}$
$\sin(ax)$	$\frac{a}{s^2+a^2}$
$\cos(ax)$	$\frac{s}{s^2+a^2}$
$x \sin(ax)$	$\frac{2as}{(s^2+a^2)^2}$
$x \cos(ax)$	$\frac{s^2-a^2}{(s^2+a^2)^2}$
$e^{ax} \sin(bx)$	$\frac{b}{(s-a)^2+b^2}$
$e^{ax} \cos(bx)$	$\frac{s-a}{(s-a)^2+b^2}$
$\text{sh}(ax)$	$\frac{a}{s^2-a^2}$
$\text{ch}(ax)$	$\frac{s}{s^2-a^2}$
$H_a(x)$	$\frac{e^{-as}}{s}$

Svojstva konvolucije:

$$1) f_1 * (f_2 * f_3) = (f_1 * f_2) * f_3$$

$$2) f_1 * f_2 = f_2 * f_1$$

$$\mathcal{L}(f)(s) := \int_0^{\infty} e^{-sx} f(x) dx$$

Svojstva Laplaceove transformacije:

$$1) \mathcal{L}(\alpha f + \beta g) = \alpha \mathcal{L}(f) + \beta \mathcal{L}(g)$$

$$2) \mathcal{L}(f')(s) = s\mathcal{L}(f)(s) - f(0)$$

$$3) \mathcal{L}(f^{(n)})(s) = s^n \mathcal{L}(f)(s) - \sum_{k=0}^{n-1} s^{n-1-k} f^{(k)}(0)$$

$$4) \mathcal{L}(e^{ax} f(x))(s) = \mathcal{L}(f)(s-a)$$

$$5) \mathcal{L}(x^n f(x))(s) = (-1)^n (\mathcal{L}(f))^{(n)}(s)$$

$$6) \mathcal{L}f(ax)(s) = \frac{1}{a} \mathcal{L}(f)\left(\frac{s}{a}\right)$$

$$7) \mathcal{L}(f(x-a) H_a(x))(s) = e^{-as} \mathcal{L}(f)(s)$$

$$8) \mathcal{L}f_1(s) \mathcal{L}f_2(s) = \mathcal{L}(f_1 * f_2)(s)$$

Tablica integrala:

$$\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1} + C \quad (\alpha \neq -1)$$

$$\int \frac{dx}{x} = \ln|x| + C$$

$$\int e^x dx = e^x + C$$

$$\int a^x dx = \frac{a^x}{\ln a} + C \quad (a > 0, a \neq 1)$$

$$\int \cos x dx = \sin x + C$$

$$\int \sin x dx = -\cos x + C$$

$$\int \frac{1}{\sqrt{a^2-x^2}} dx = \arcsin \frac{x}{a} + C \quad (a > 0)$$

$$\int \frac{1}{a^2+x^2} dx = \frac{1}{a} \operatorname{arctg} \frac{x}{a} + C \quad (a > 0)$$

$$\int \sqrt{a^2+x^2} dx = \ln(x + \sqrt{a^2+x^2}) + C \quad (a > 0)$$

$$\int \frac{1}{\sqrt{x^2-a^2}} dx = \ln|x + \sqrt{x^2-a^2}| + C \quad (a > 0)$$

$$\int \frac{1}{a^2-x^2} dx = \frac{1}{2a} \ln \left| \frac{x+a}{x-a} \right| + C \quad (a > 0)$$

$$\int \frac{1}{\cos^2 x} dx = \operatorname{tg} x + C$$

$$\int \frac{1}{\sin^2 x} dx = -\operatorname{ctg} x + C$$

$$\int \operatorname{ch} x dx = \operatorname{sh} x + C$$

$$\int \operatorname{sh} x dx = \operatorname{ch} x + C$$

$$\int \frac{1}{\operatorname{ch}^2 x} dx = \operatorname{th} x + C \quad \int \frac{1}{\operatorname{sh}^2 x} dx = \operatorname{cth} x + C$$

$f(x)$	$\mathcal{F}(f)(\xi)$
δ_0	1
$\chi_{[a,b]}$	$\frac{\sin(\pi(b-a)\xi)}{\pi\xi} e^{-i\pi(a+b)\xi}$
$e^{-ax} \mathbb{H}(x), \operatorname{Re}(a) > 0$	$\frac{1}{a+2\pi i\xi}$
$\frac{x^k}{k!} e^{-ax} \mathbb{H}(x), \operatorname{Re}(a) > 0$	$\frac{1}{(a+2\pi i\xi)^k}$
$e^{-a x }, \operatorname{Re}(a) > 0$	$\frac{2a}{a^2+4\pi^2\xi^2}$
$e^{-ax^2}, a > 0$	$\sqrt{\frac{\pi}{a}} e^{-\frac{\pi^2}{a}\xi^2}$
$\cos(ax)$	$\left(\delta_{\{\frac{a}{2\pi}\}} + \delta_{\{-\frac{a}{2\pi}\}}\right) / 2$
$\sin(ax)$	$\left(\delta_{\{\frac{a}{2\pi}\}} - \delta_{\{-\frac{a}{2\pi}\}}\right) / (2i)$
$\cos(ax^2)$	$\sqrt{\frac{\pi}{a}} \cos\left(\frac{\pi^2\xi^2}{a} - \frac{\pi}{4}\right)$
$\sin(ax^2)$	$-\sqrt{\frac{\pi}{a}} \sin\left(\frac{\pi^2\xi^2}{a} - \frac{\pi}{4}\right)$
$\text{v.p. } \frac{1}{x}$	$-i\pi \operatorname{sgn}(\xi)$
e^{-ix^2}	$\sqrt{2\pi}(1/2 - i/2)e^{i\pi^2\xi^2}$
$e^{-ax^2}, \operatorname{Re}(a) \geq 0$	$\sqrt{\frac{\pi}{ a }} e^{-i\frac{\theta_0}{2}} e^{-\frac{\pi^2\xi^2}{a}}, \theta_0 = \operatorname{arctg}(\operatorname{Im}(a)/\operatorname{Re}(a))$

Svojstva Fourierove transformacije:

- $\mathcal{F}(\alpha f + \beta g) = \alpha \mathcal{F}(f) + \beta \mathcal{F}(g)$
- $\mathcal{F}(\tau_a f)(\xi) = e^{-2\pi i a \xi} \mathcal{F}(f)(\xi)$
- $\mathcal{F}(f(ax))(\xi) = \frac{1}{|a|} \mathcal{F}\left(\frac{\xi}{a}\right)$
- $\mathcal{F}(\mathcal{F}(f))(\xi) = f(-\xi)$
- $\mathcal{F}(f^{(n)})(\xi) = (2\pi i \xi)^n \mathcal{F}(f)(\xi)$
- $\mathcal{F}(x^n f(x))(\xi) = \left(\frac{i}{2\pi}\right)^n \mathcal{F}(f)^{(n)}(\xi)$
- $\mathcal{F}(f * g)(\xi) = \mathcal{F}(f)\mathcal{F}(g)$