
Matematička teorija računarstva

Predavanja 14

Matko Botinčan

PMF – Matematički odjel

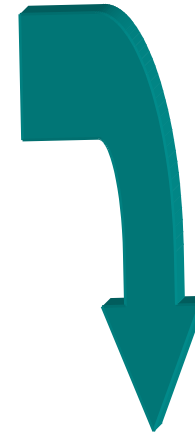
31.01.2007.

Izvori materijala za ovo predavanje

- X. Jiao – CS 3240: Languages and Computation
 - http://www-static.cc.gatech.edu/classes/AY2007/cs3240_fall/
 - T. K. Prasad – CS 780: Compiler Design and Construction I
 - <http://www.cs.wright.edu/~tkprasad/courses/cs780/cs780.html>
 - J. Riely – CSC347/447: Concepts of Programming Languages
 - <http://condor.depaul.edu/~jriely/csc447winter2007/index.html>
 - D. Stotts – COMP 144: Programming Language Concepts
 - <http://www.cs.unc.edu/~stotts/COMP144/>
 - Q. Yi – CS5363: Programming Languages and Compilers
 - <http://www.cs.utsa.edu/~qingyi/cs5363/>
-

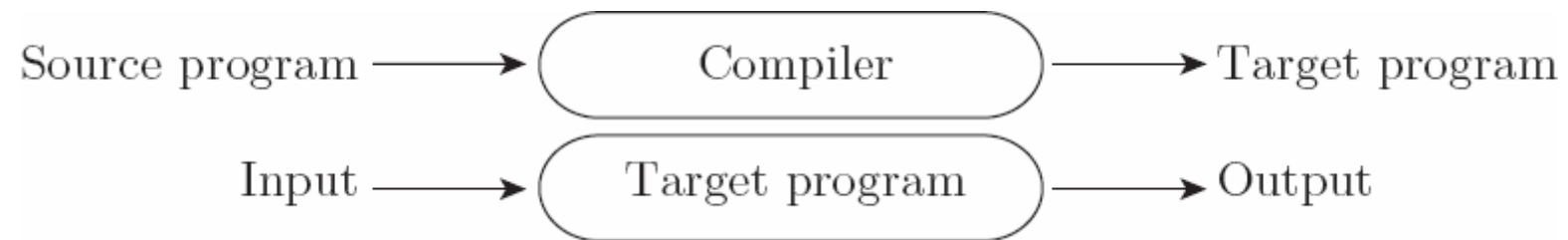
Prevođenje programa

```
program gcd(input, output);  
var i, j: integer;  
begin  
    read(i, j);  
    while i <> j do  
        if i > j then i := i - j;  
        else j := j - i;  
    writeln(i)  
end.
```

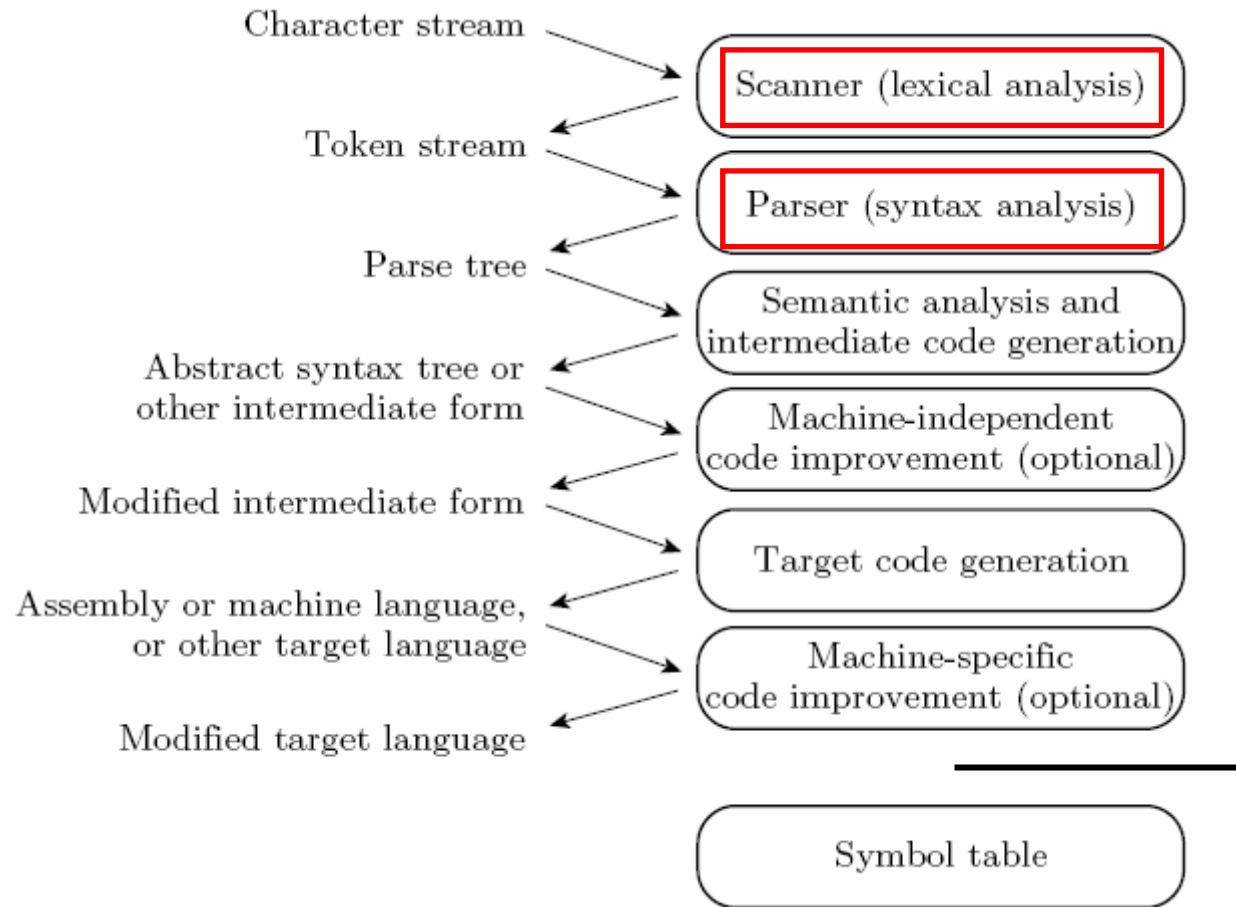


```
27bdffd0 afbf0014 0c1002a8 00000000 0c1002a8 afa2001c 8fa4001c  
00401825 10820008 0064082a 10200003 00000000 10000002 00832023  
00641823 1483fffa 0064082a 0c1002b2 00000000 8fbf0014 27bd0020  
03e00008 00001025
```

Prevođenje programa



Faze prevodenja programa



Scanner/Parser

```
main() {  
    int a,b;  
    a = b;  
}
```

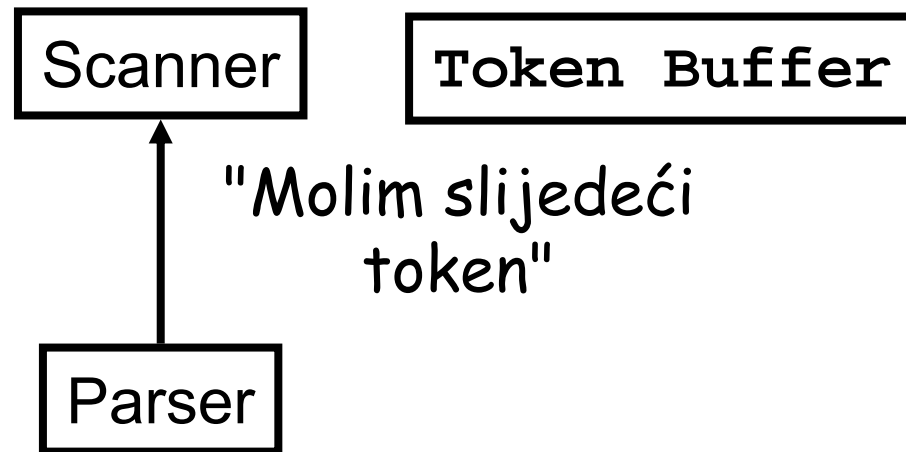
Scanner

Token Buffer

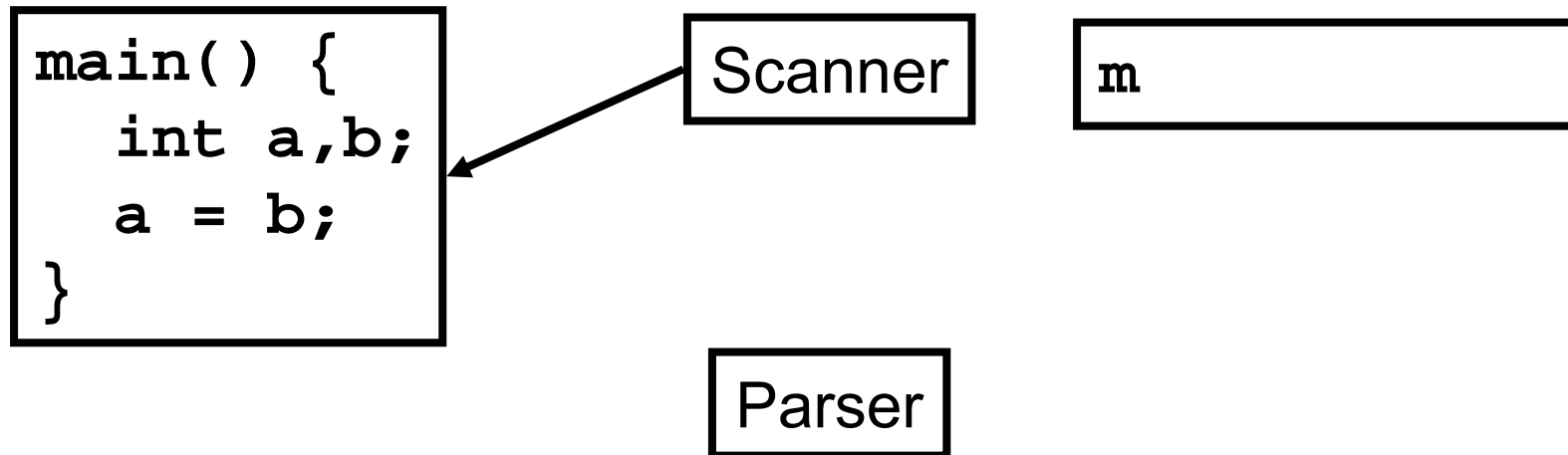
Parser

Scanner/Parser

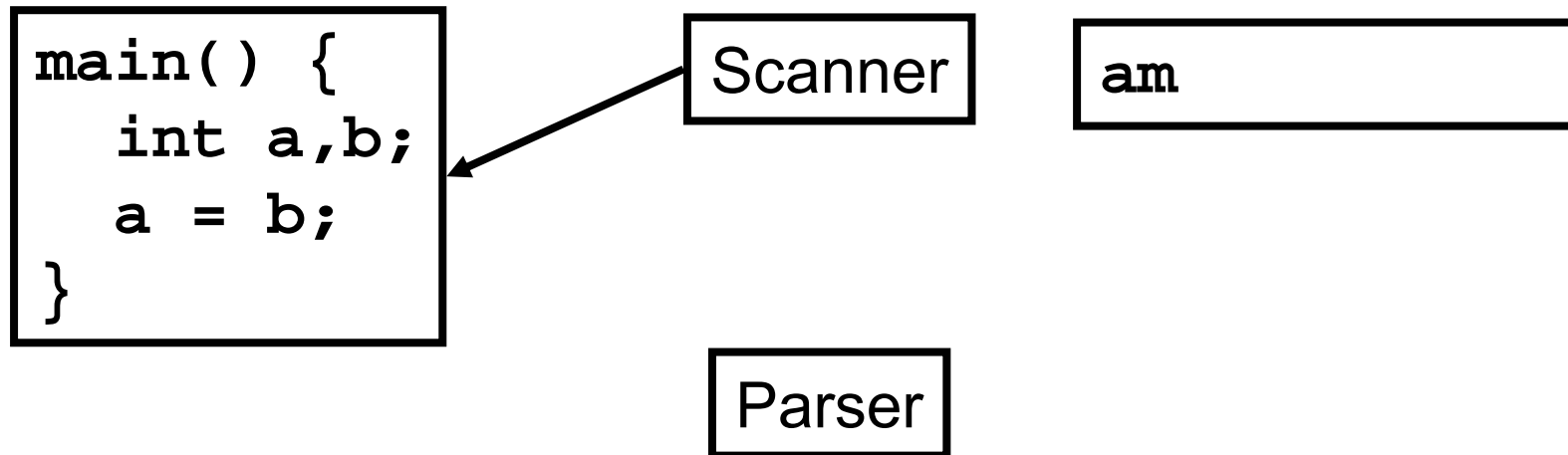
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main() {  
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    a = b;  
}
```



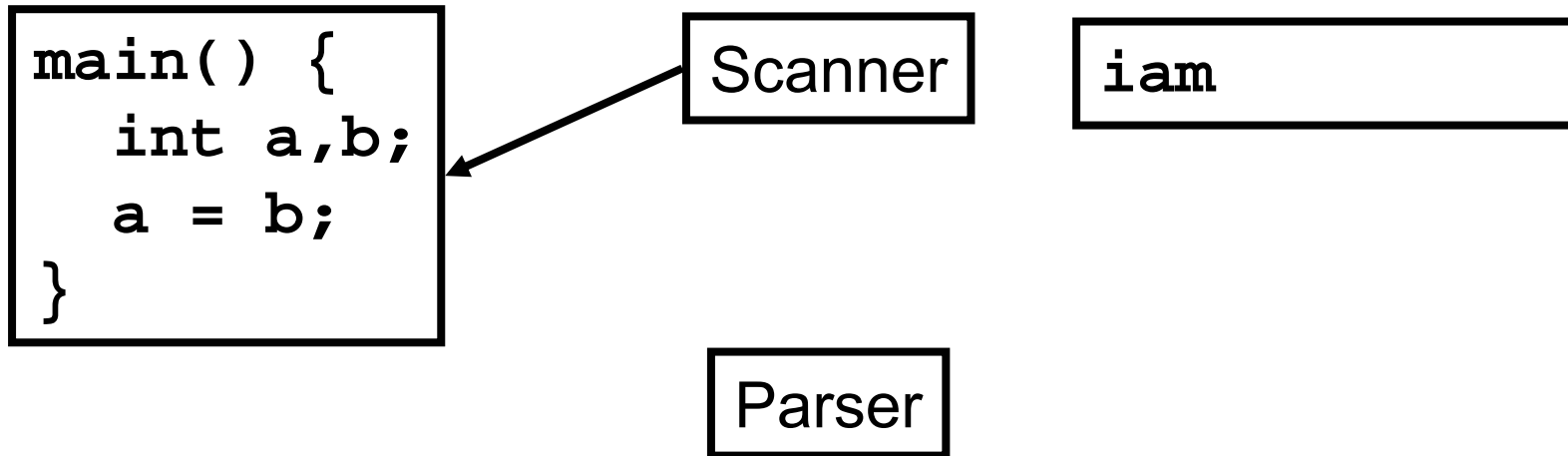
Scanner/Parser



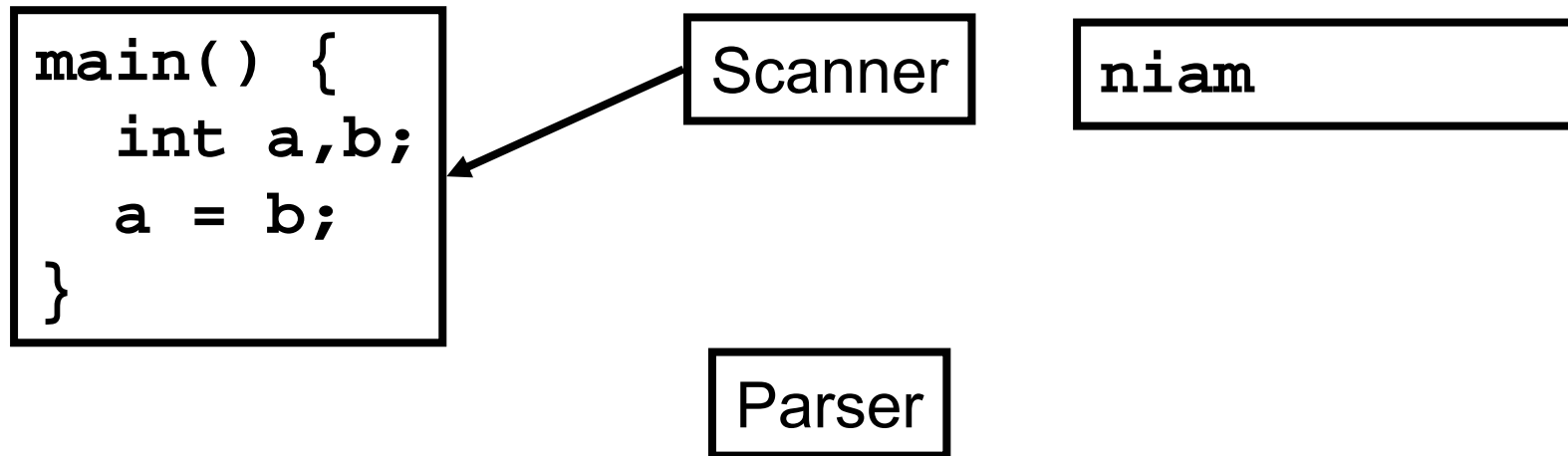
Scanner/Parser



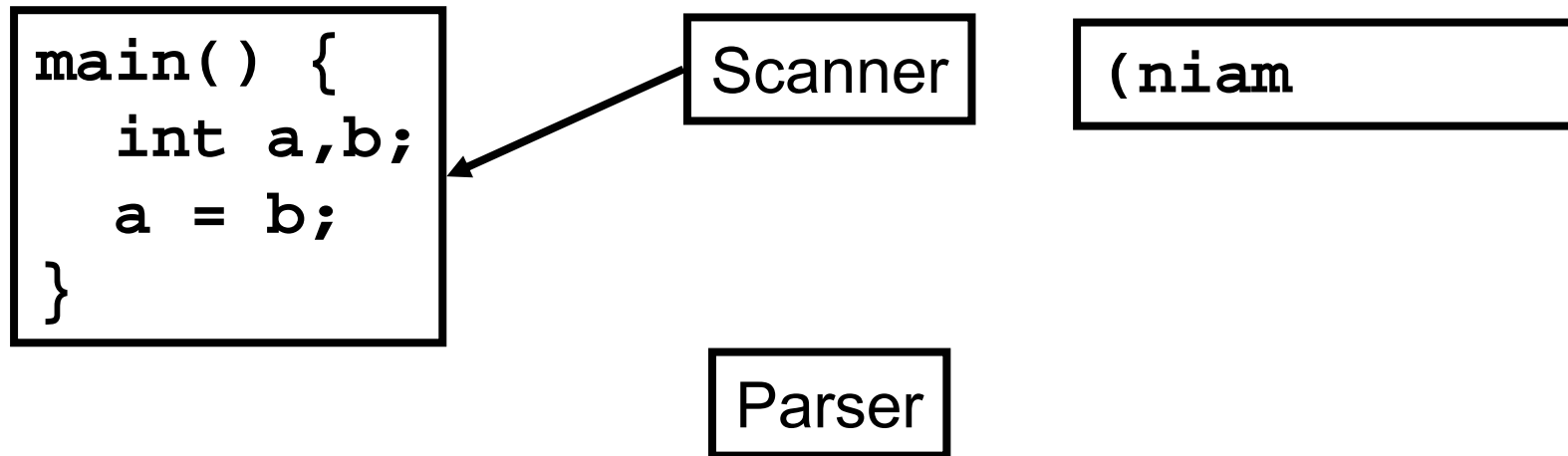
Scanner/Parser



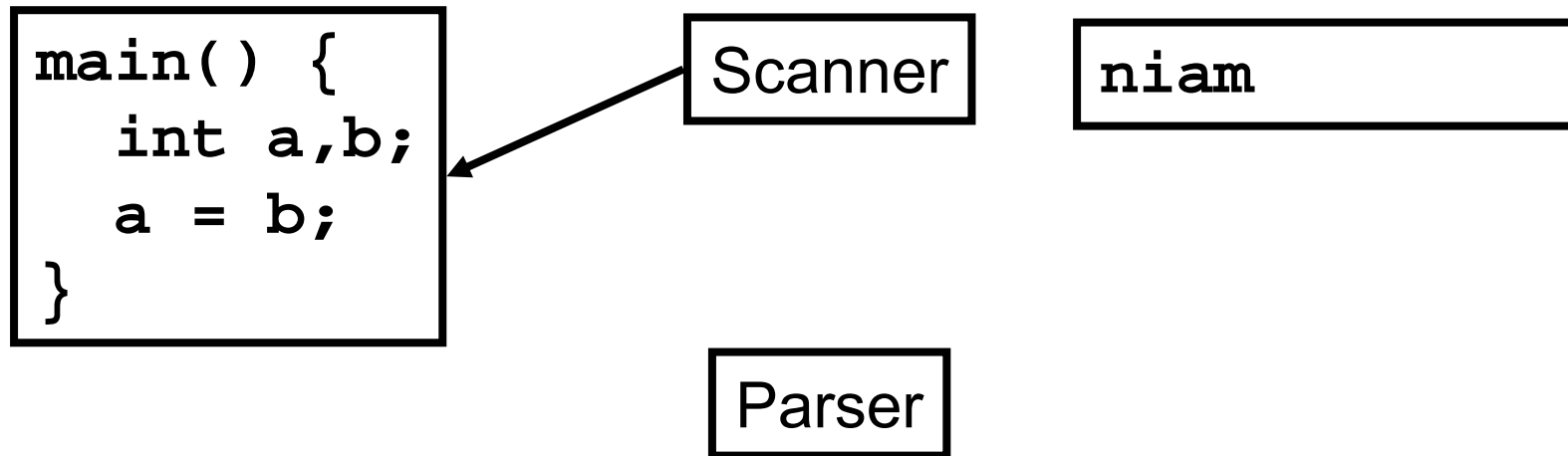
Scanner/Parser



Scanner/Parser

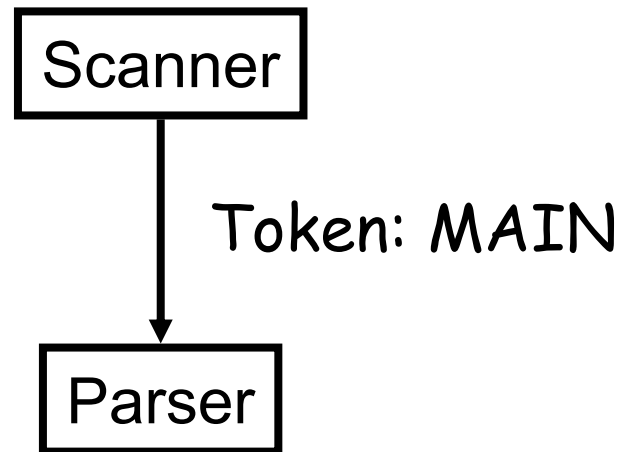


Scanner/Parser



Scanner/Parser

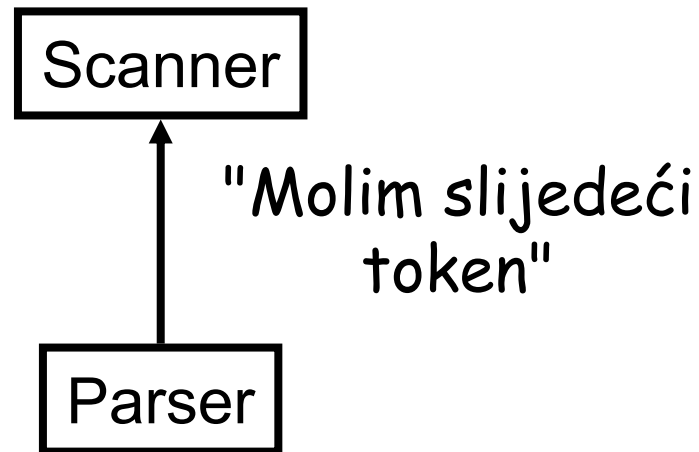
```
main() {  
    int a,b;  
    a = b;  
}
```



<C-PROG> → MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>

Scanner/Parser

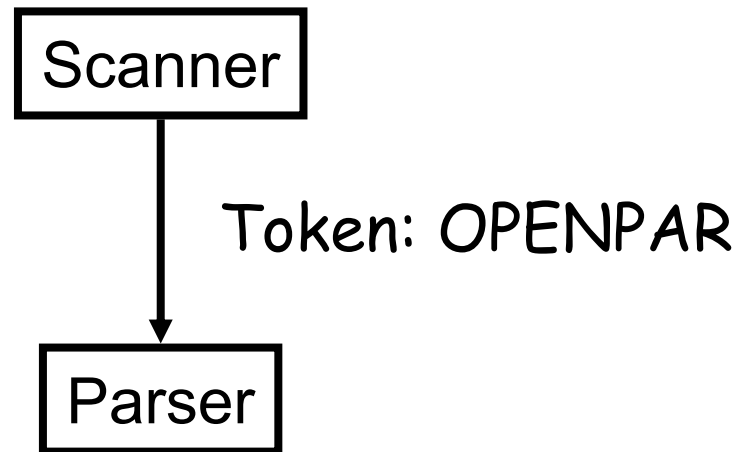
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main() {  
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    a = b;  
}
```



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Scanner/Parser

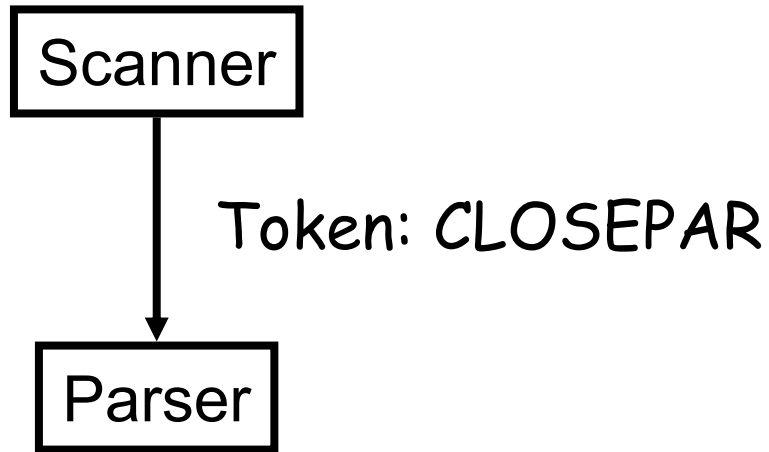
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}
```



<C-PROG> → MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>

Scanner/Parser

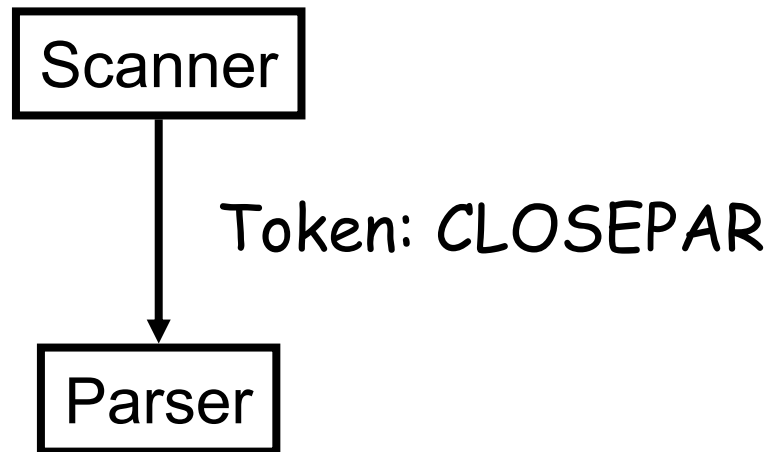
```
main() {  
    int a,b;  
    a = b;  
}
```



`<C-PROG> → MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>`
`<PARAMETERS> → NULL`

Scanner/Parser

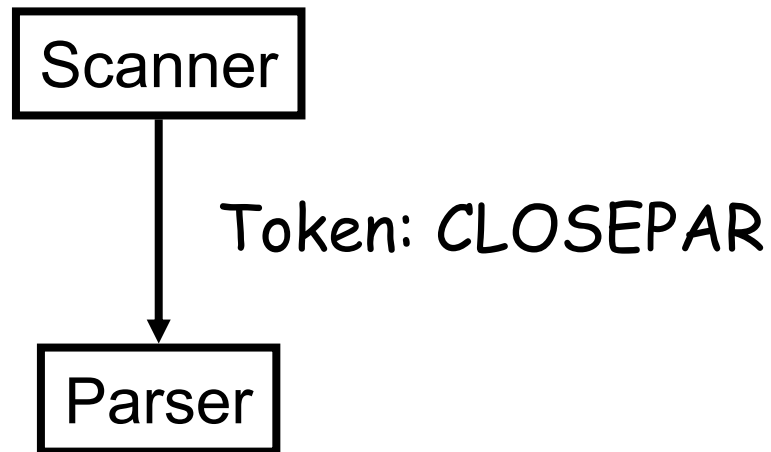
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    int a,b;  
    a = b;  
}
```



`<C-PROG>` → `MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>`
`<PARAMETERS>` → `NULL`

Scanner/Parser

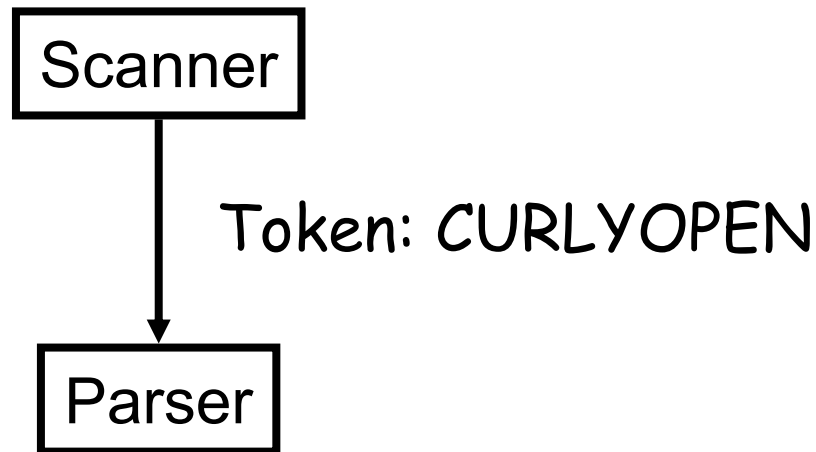
```
main() {  
    int a,b;  
    a = b;  
}
```



<C-PROG> → MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>

Scanner/Parser

```
main() {  
    int a,b;  
    a = b;  
}
```

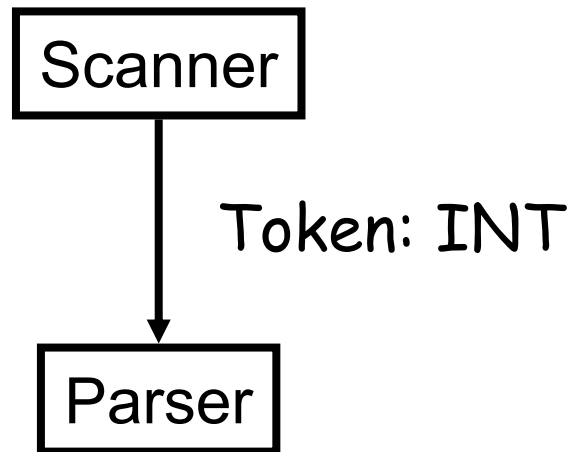


<C-PROG> → MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>

<MAIN-BODY> → CURLYOPEN <DECL-STMT> <ASSIGN-STMT> CURLYCLOSE

Scanner/Parser

```
main() {  
    int a,b;  
    a = b;  
}
```



`<C-PROG> → MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>`

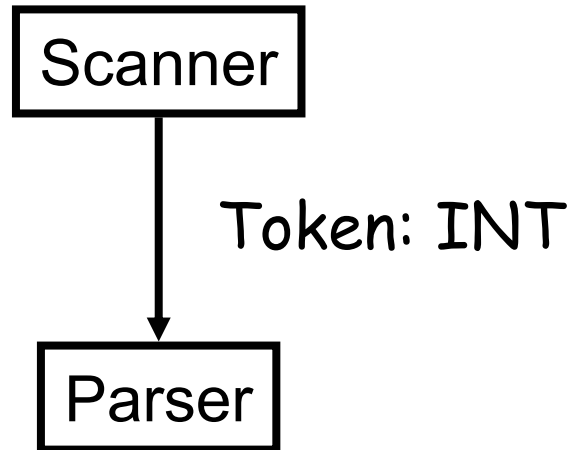
`<MAIN-BODY> → CURLYOPEN <DECL-STMT> <ASSIGN-STMT> CURLYCLOSE`

`<DECL-STMT> → <TYPE>VAR<VAR-LIST>;`

`<TYPE> → INT`

Scanner/Parser

```
main() {  
    int a,b;  
    a = b;  
}
```



`<C-PROG>` → `MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>`

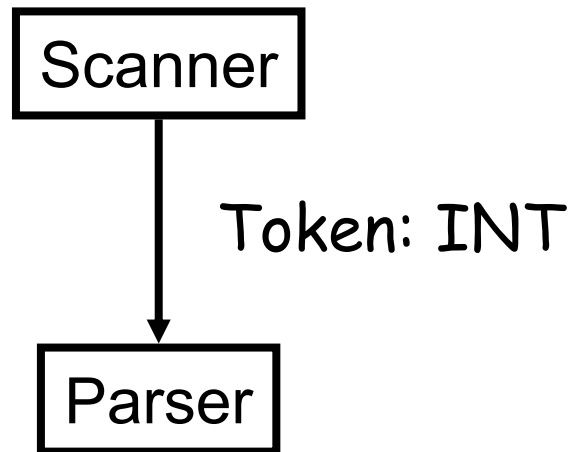
`<MAIN-BODY>` → `CURLYOPEN <DECL-STMT> <ASSIGN-STMT> CURLYCLOSE`

`<DECL-STMT>` → `<TYPE>VAR<VAR-LIST>;`

`<TYPE>` → `INT`

Scanner/Parser

```
main() {  
    int a,b;  
    a = b;  
}
```



`<C-PROG>` → `MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>`

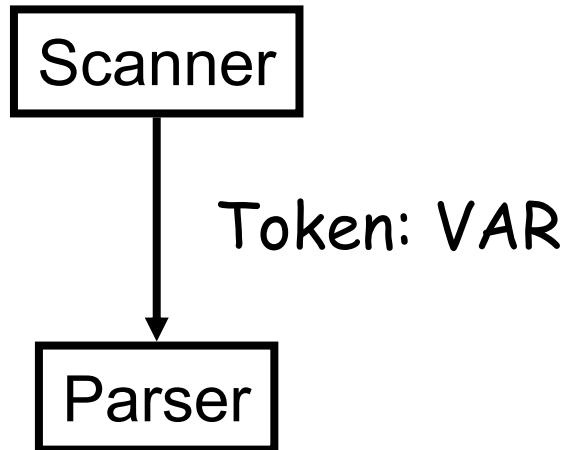
`<MAIN-BODY>` → `CURLYOPEN <DECL-STMT> <ASSIGN-STMT> CURLYCLOSE`

`<DECL-STMT>` → `<TYPE>VAR<VAR-LIST>;`

`<TYPE>` → `INT`

Scanner/Parser

```
main() {  
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<MAIN-BODY> → CURLYOPEN <DECL-STMT> <ASSIGN-STMT> CURLYCLOSE

<DECL-STMT> → <TYPE>VAR<VAR-LIST>;

<VARLIST> → , VAR <VARLIST>

<VARLIST> → NULL

Scanner/Parser

```
main() {  
    int a,b;  
    a = b;  
}
```

Scanner

Token: ',' [COMMA]

Parser

<C-PROG> → MAIN OPENPAR <PARAMETERS> CLOSEPAR <MAIN-BODY>

<MAIN-BODY> → CURLYOPEN <DECL-STMT> <ASSIGN-STMT> CURLYCLOSE

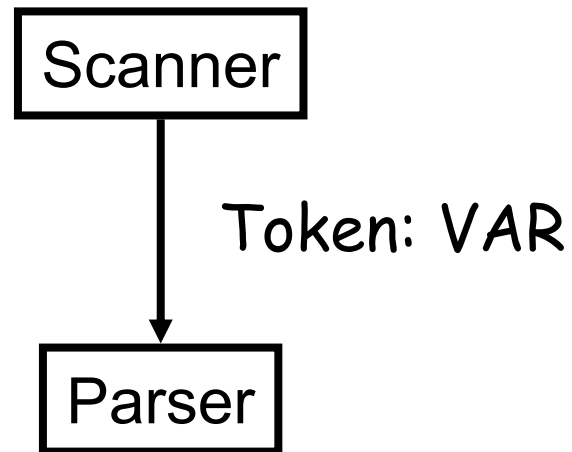
<DECL-STMT> → <TYPE>VAR<VAR-LIST>;

<VARLIST> → , VAR <VARLIST>

<VARLIST> → NULL

Scanner/Parser

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main() {  
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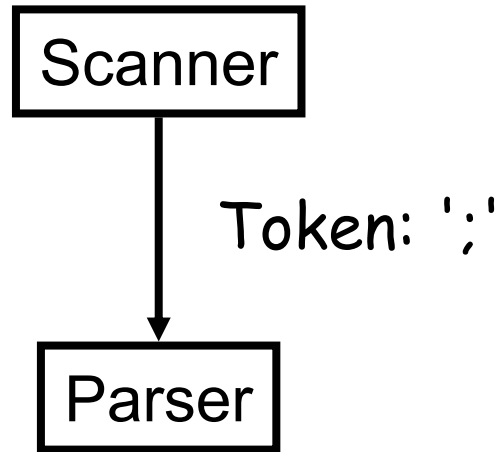
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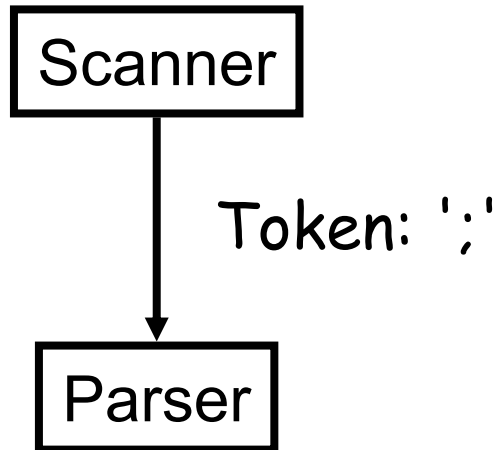
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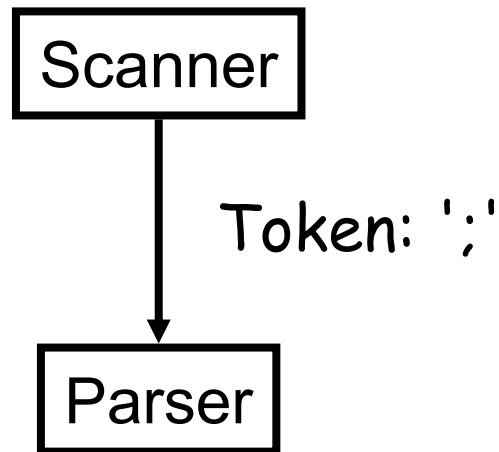
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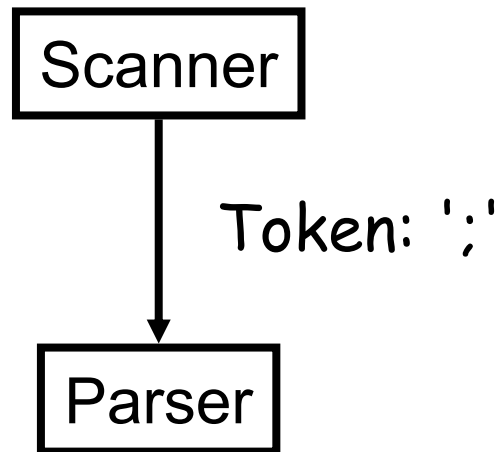
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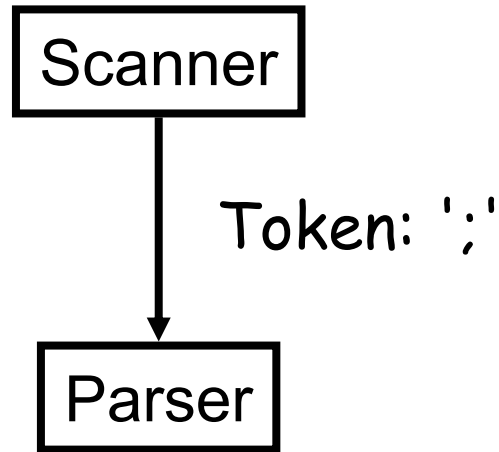
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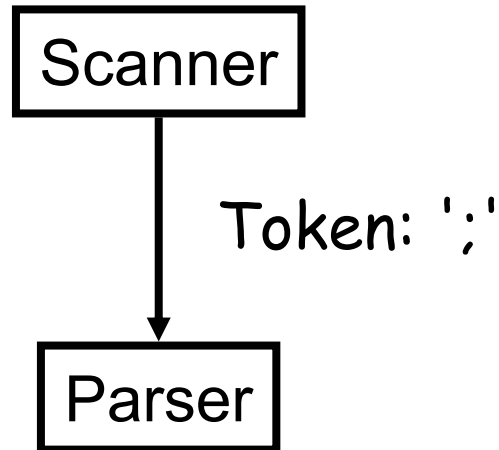
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```
main() {  
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```



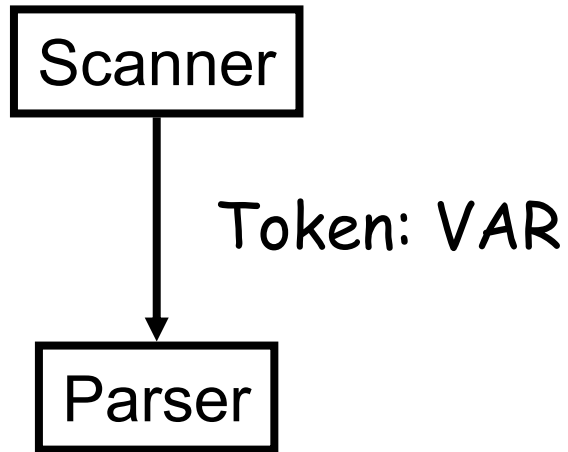
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Scanner/Parser

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$\langle \text{C-PROG} \rangle \rightarrow \text{MAIN OPENPAR} \langle \text{PARAMETERS} \rangle \text{ CLOSEPAR} \langle \text{MAIN-BODY} \rangle$

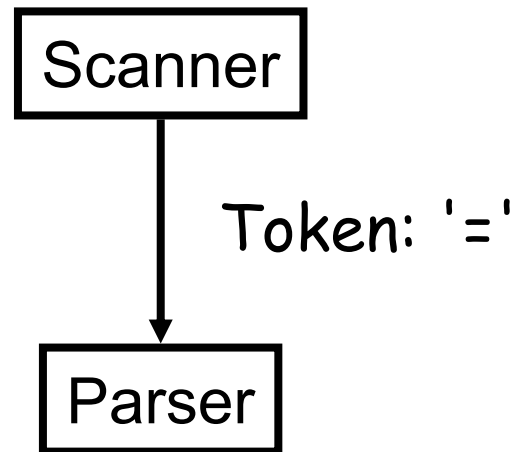
$\langle \text{MAIN-BODY} \rangle \rightarrow \text{CURLYOPEN} \langle \text{DECL-STMT} \rangle \langle \text{ASSIGN-STMT} \rangle \text{ CURLYCLOSE}$

$\langle \text{ASSIGN-STMT} \rangle \rightarrow \text{VAR} = \langle \text{EXPR} \rangle ;$

$\langle \text{EXPR} \rangle \rightarrow \text{VAR}$

Scanner/Parser

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main() {  
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$\langle \text{C-PROG} \rangle \rightarrow \text{MAIN OPENPAR} \langle \text{PARAMETERS} \rangle \text{ CLOSEPAR} \langle \text{MAIN-BODY} \rangle$

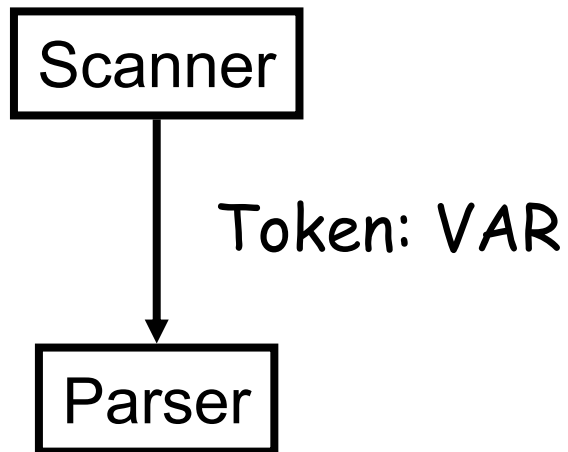
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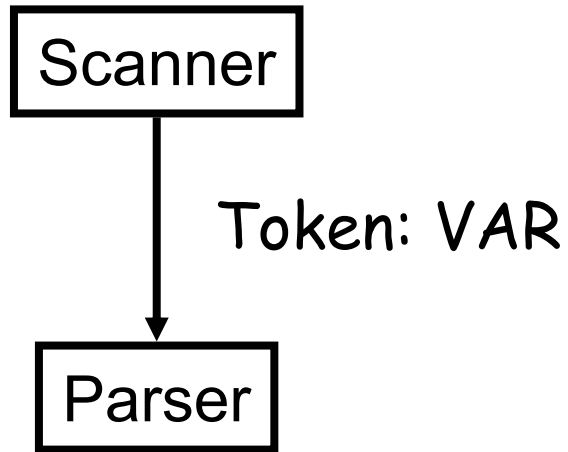
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Scanner/Parser

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$\langle \text{C-PROG} \rangle \rightarrow \text{MAIN OPENPAR } \langle \text{PARAMETERS} \rangle \text{ CLOSEPAR } \langle \text{MAIN-BODY} \rangle$

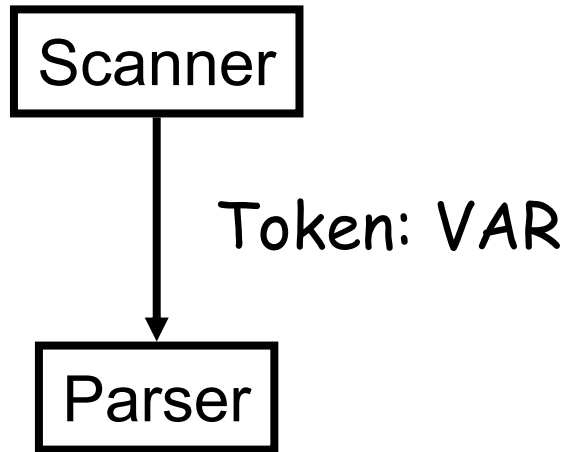
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Scanner/Parser

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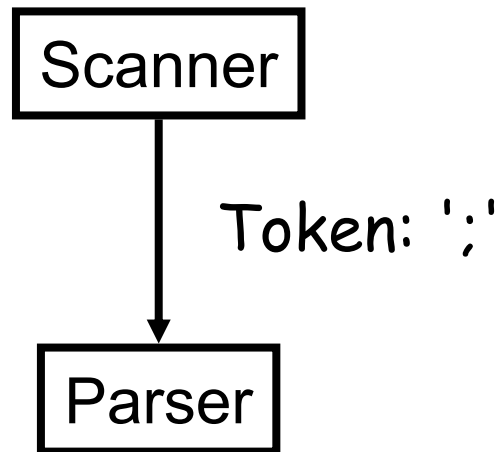
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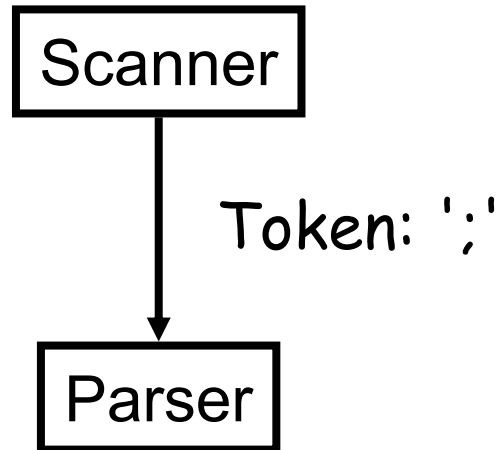
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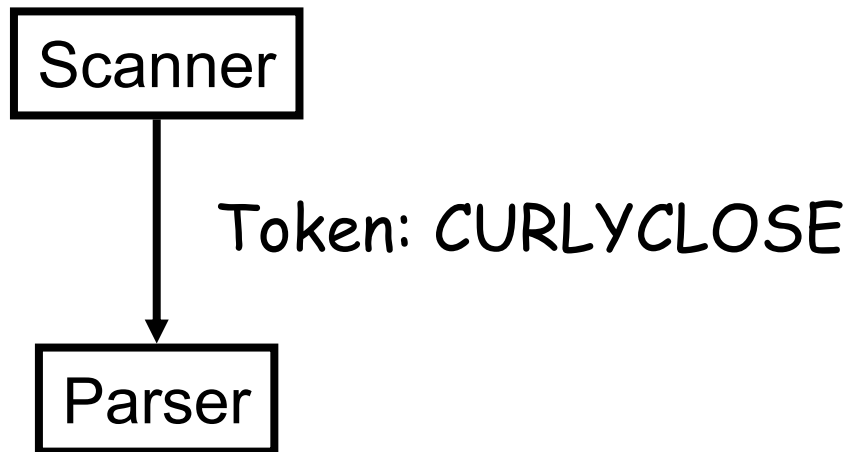
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<MAIN-BODY> → CURLYOPEN <DECL-STMT> <ASSIGN-STMT> CURLYCLOSE

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Scanner/Parser

```
main() {  
    int a,b;  
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}
```



`<C-PROG>` → `MAIN` `OPENPAR` `<PARAMETERS>` `CLOSEPAR` `<MAIN-BODY>`

`<MAIN-BODY>` → `CURLYOPEN` `<DECL-STMT>` `<ASSIGN-STMT>` `CURLYCLOSE`

Primjer (leksička i sintaktička analiza)

■ Program GCD (Pascal):

```
program gcd(input, output);  
var i, j : integer;  
begin  
    read(i, j);  
    while i <> j do  
        if i > j then i := i - j  
        else j := j - i;  
    writeln(i)  
end.
```

Leksička analiza

■ Tokeni u programu GCD:

```
program gcd      (      input      ,      output      )      ;  
var      i      ,      j      :      integer      ;      begin  
read      (      i      ,      j      )      ;      while  
i      <>      j      do      if      i      >      j  
then      i      :=      i      -      j      else      j  
:=      j      -      i      ;      writeln      (      i  
)      end      .
```

KS gramatika i parsiranje

- KS gramatika za Pascal programe:

$program \longrightarrow PROGRAM\ id\ (id\ more_ids) ;\ block .$

where

$block \longrightarrow labels\ constants\ types\ variables\ subroutines\ BEGIN\ stmt\ more_stmts\ END$

and

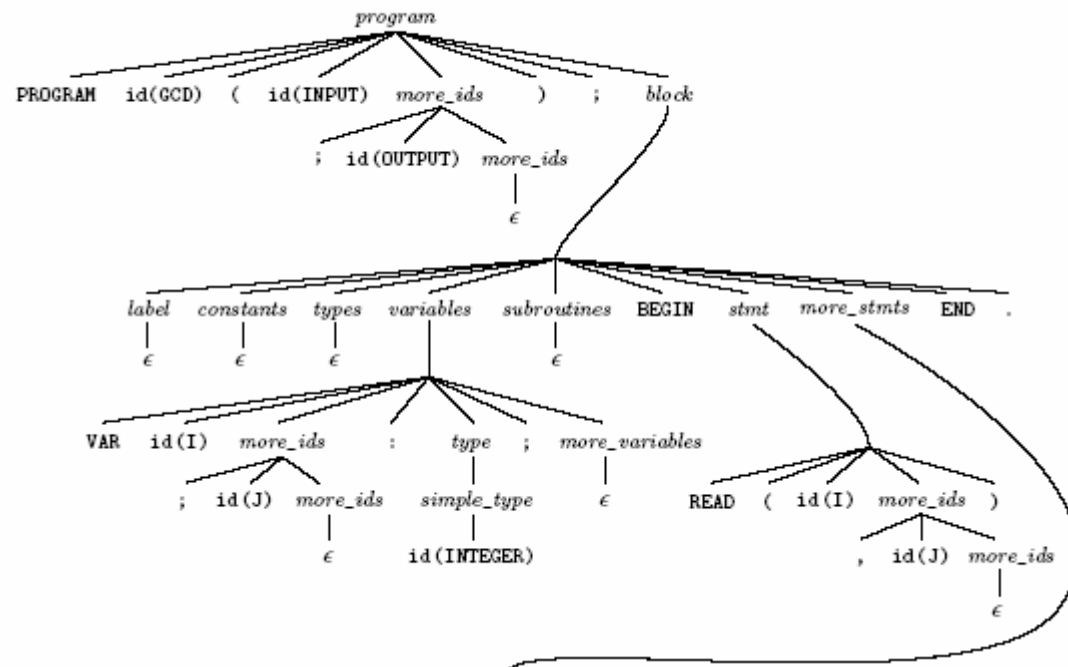
$more_ids \longrightarrow ,\ id\ more_ids$

or

$more_ids \longrightarrow \epsilon$

KS gramatika i parsiranje

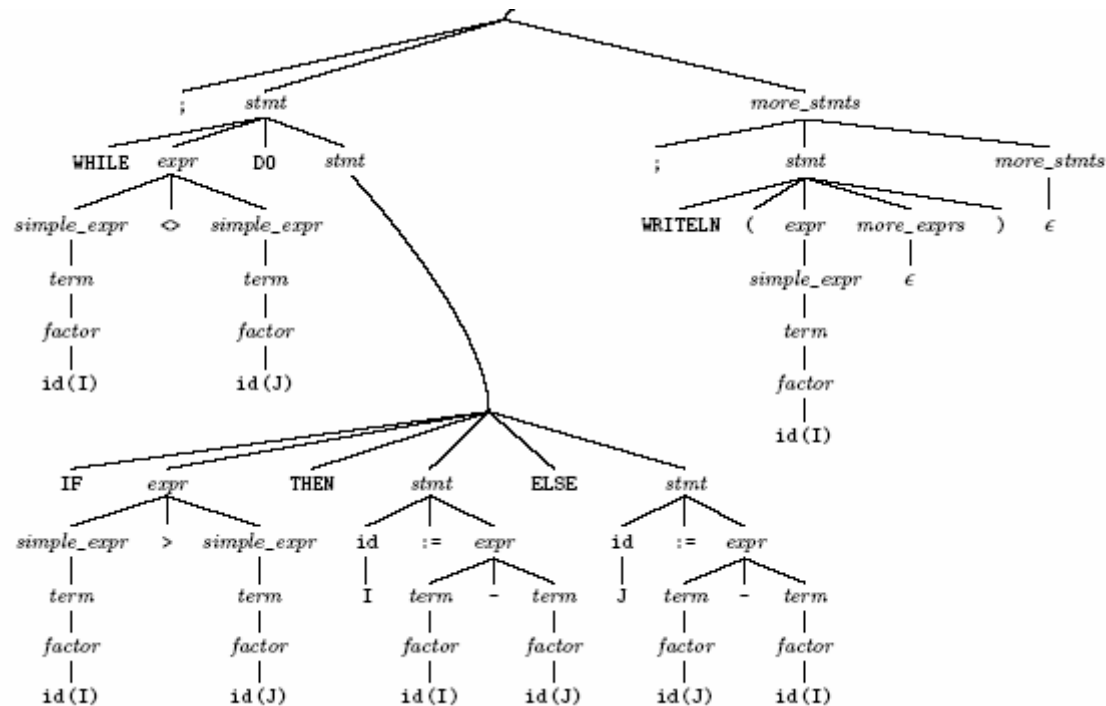
- Stablo izvoda za program GCD:



Na idućem slideu

KS gramatika i parsiranje

- Stablo izvoda za program GCD:



KS gramatika i parsiranje

- Apstraktno sintaksno stablo za program GCD:

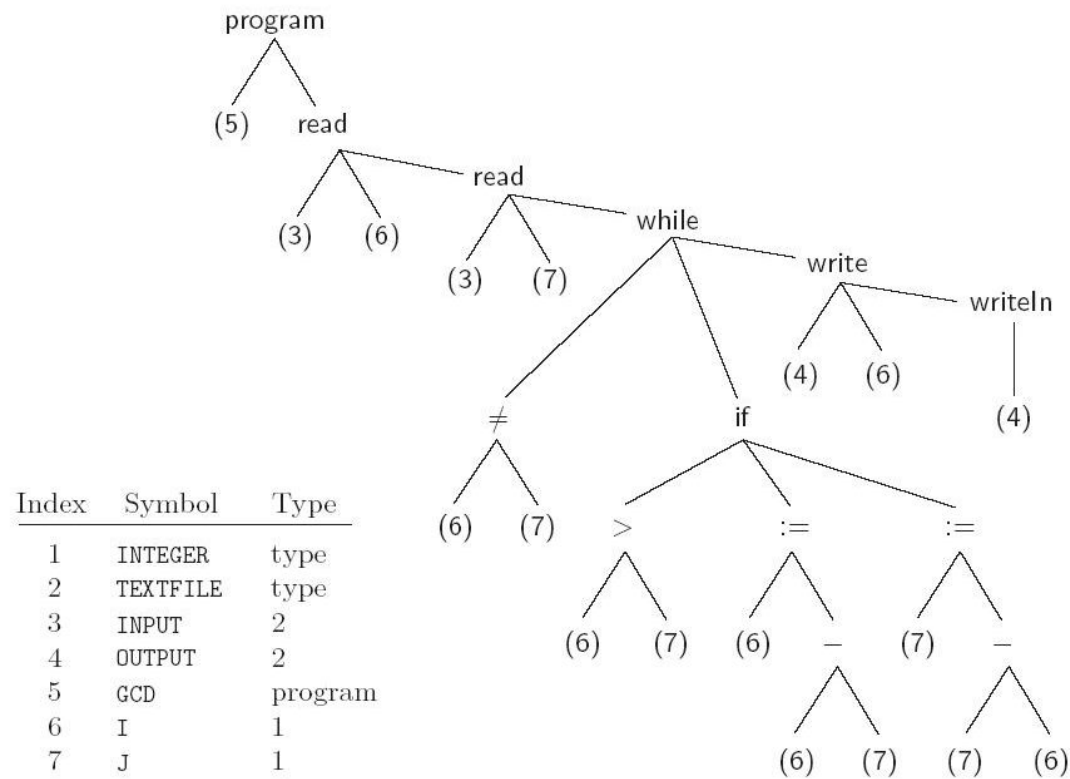


Figure 1.4: Syntax tree and symbol table for the GCD program.



Leksička analiza

Regularni izrazi

- Leksička struktura tokena opisuje se regularnim izrazima:
- Primjer (cijeli broj bez predznaka u Pascalu):

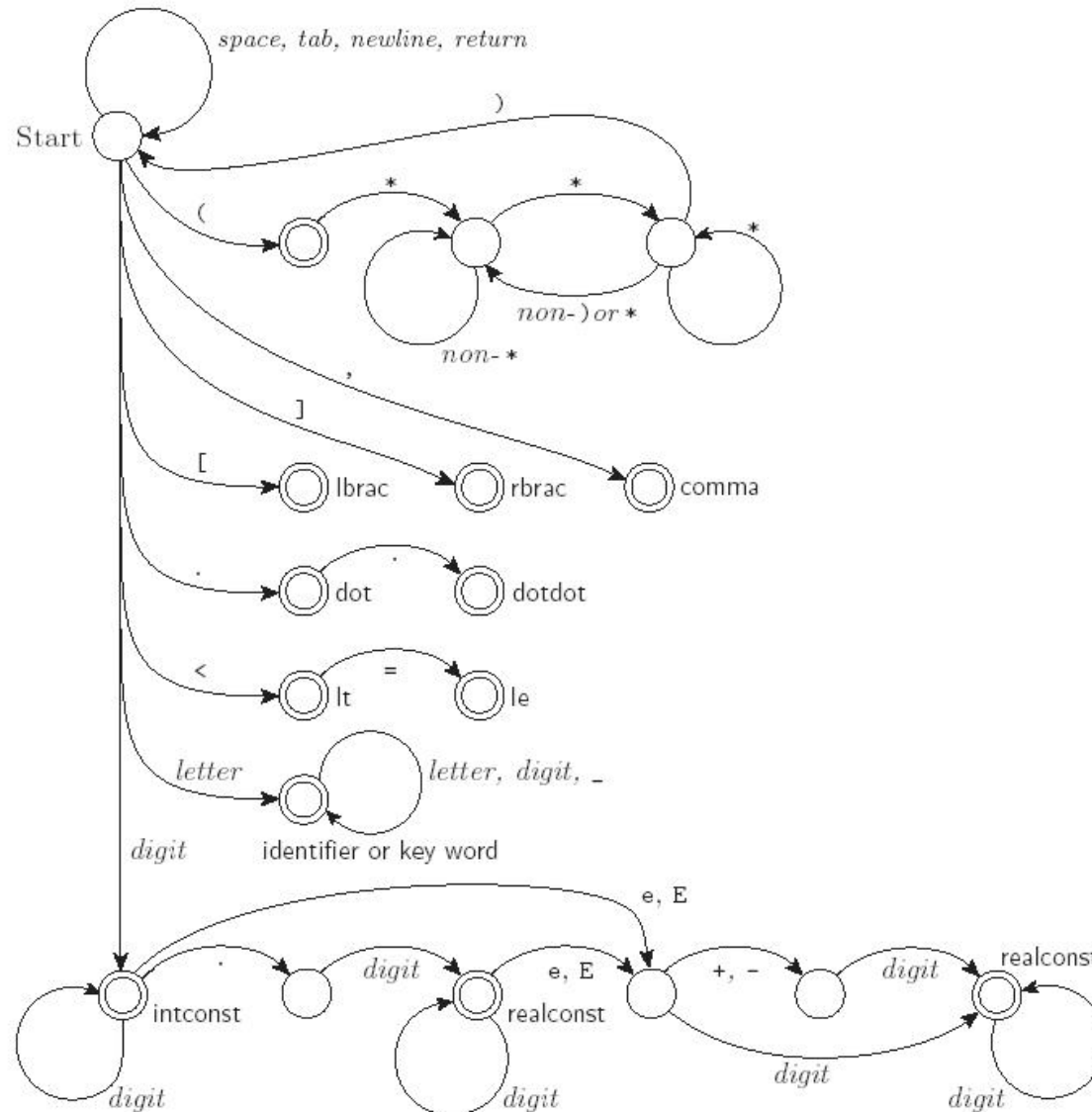
$digit \longrightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$

$unsigned_integer \longrightarrow digit\ digit^*$

$unsigned_number \longrightarrow unsigned_integer \left((\cdot\ unsigned_integer) \mid \epsilon \right)$
 $\left(((e \mid E) (+ \mid - \mid \epsilon) unsigned_integer) \mid \epsilon \right)$

Scanner

- Iz danog regularnog izraza moguće je automatski generirati konačni automat



Problem

- Što u ovakvom slučaju?

```
void f (float* p, float y)
{
    float x;
    x = y/*p;
}
```

(/* je delimiter za komentare u C-u)

Lookahead

- Kod nekih jezika odluku o tipu tokena nije moguće donijeti samo na temelju početnog prefiksa tokena
- Još jedan primjer: FORTRAN
 - Varijable ne trebaju biti eksplicitno deklarirane
 - Implicitno tipiziranje u ovisnosti u prvom karakteru
 - Realni brojevi počinju s A-H ili O-Z
 - Cijeli brojevi počinju s I-N
 - (Dizajneri jezika željeli oponašati standardne matematičke konvencije)

Lookahead

- Tipičan izgled petlje u FORTRAN-u:

```
DO 10 I = 1,10000
```

```
...
```

```
...
```

```
10 CONTINUE
```

- Ekvivalent u C-u:

```
for (i=1; i<=10000; ++i) {
```

```
...
```

```
}
```

Lookahead

- Sve praznine se ignoriraju, pa je

```
DO 10 I = 1, 100000
```

- ekvivalentno

```
DO10I=1,100000
```

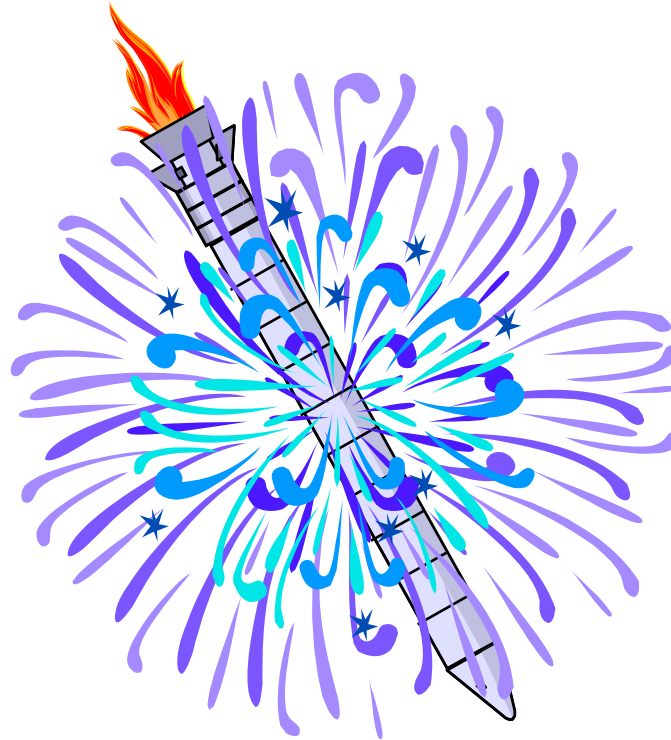
- što je pak različito od

```
DO 10 I = 1. 100000
```

tj.

```
DO10I=1.100000
```

Rezultat





Sintaktička analiza

Kontekstno slobodni jezici

■ Primjer: Gramatika aritmetičkih izraza

1. $expr \longrightarrow term \mid expr \text{ add_op } term$

2. $term \longrightarrow factor \mid term \text{ mult_op } factor$

3. $factor \longrightarrow id \mid number \mid - factor \mid (expr)$

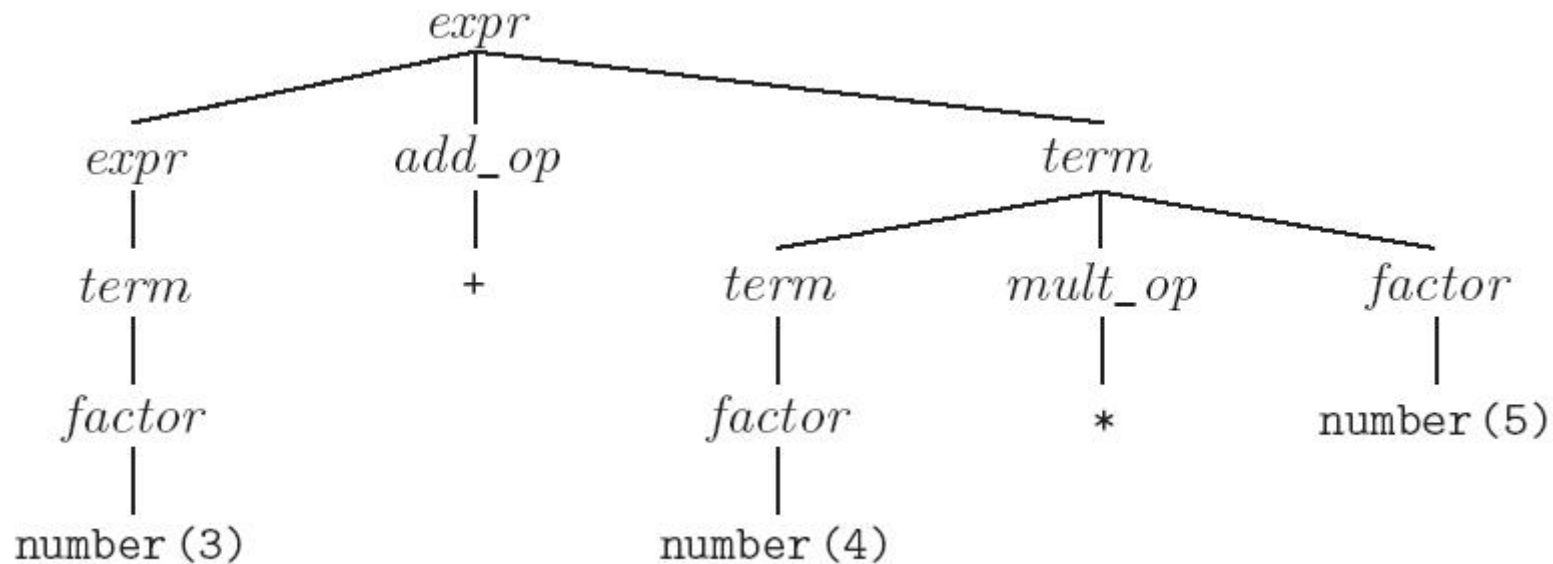
4. $add_op \longrightarrow + \mid -$

5. $mult_op \longrightarrow * \mid /$

Kontekstno slobodni jezici

- Primjer: Stablo izvoda za izraz

3 + 4 * 5



Još jedan primjer – XML i DTD

- DTD je KS gramatika za opis strukture neke klase XML dokumenata
- Primjer:

```
<?xml version="1.0"?>
<!DOCTYPE oldjoke [
  <!ELEMENT oldjoke (burns+, allen, applause?)>
  <!ELEMENT burns (#PCDATA | quote)*>
  <!ELEMENT allen (#PCDATA | quote)*>
  <!ELEMENT quote (#PCDATA)*>
  <!ELEMENT applause EMPTY>
]>
<oldjoke>
  <burns>Say <quote>goodnight</quote>,
  Gracie.</burns>
  <allen><quote>Goodnight, Gracie.</quote></allen>
  <applause />
</oldjoke>
```

Kontekstno slobodni jezici

- $L = \{w \in \text{ASCII}^* \mid w \text{ je sintaktički korektan C program}\}$
- Konstruiramo C program u ovisnosti o n iz leme o pumpanju:

$n=4$

```
void main(void)
{
  int v1;
  int v2;
  int v3;
  int v4;

  v1 = 0;
  v2 = 0;
  v3 = 0;
  v4 = 0;
}
```

Lema o pumpanju



Kontekstno slobodni jezici

- Klasa KS jezika nije dovoljna za opis svih pravila programskih jezika:
 - "svi identifikatori moraju biti deklarirani prije upotrebe":
$$L = \{ w \# w \mid w \in (a+b)^* \}$$
 - "broj formalnih parametara u deklaraciji funkcije podudara se s brojem argumenata kod funkcijskog poziva":
$$L = \{ a^m b^n c^m d^n \mid m, n \geq 1 \}$$
-

Kontekstno slobodni jezici

- "Klasa KS jezika od velike je važnosti u računarstvu"
 - Dva (kontradiktorna) problema:
 1. KS jezici nisu dovoljno snažni za opis svih pravila programskih jezika (npr. tipovnog sustava)
 2. Opis gotovo svih sintaktičkih pravila programskih jezika u pravilu ne zahtjeva punu ekspresivnost KS jezika
 - Želimo parser koji parsira ulazni program duljine n u vremenu $O(n)$
 - U praksi:
 - restriktivnije gramatike – klase $LL(k)$ i $LR(k)$
 - ekspresivnije gramatike – atribuirane, dvorazinske, W -, DCG (Prolog)
-

Top-down parsiranje

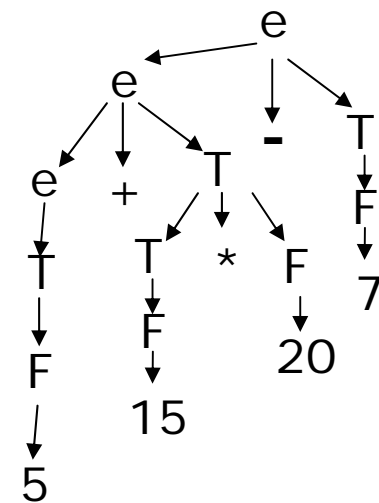
- Počevši od startnog neterminalnog simbola trebamo naći najljeviji izvod

Gramatika:

$$\begin{aligned} E &::= E + T \mid E - T \mid T \\ T &::= T * F \mid T / F \mid F \\ F &::= n \end{aligned}$$

Najljeviji izvod za $5+15*20-7$:

**$E \rightarrow E - T \rightarrow E + T - T \rightarrow T + T - T$
 $\rightarrow F + T - T \rightarrow 5 + T - T \rightarrow 5 + T * F - T \rightarrow 5 + F * F - T \rightarrow 5 + 15 * F - T$
 $\rightarrow 5 + 15 * 20 - T \rightarrow 5 + 15 * 20 - F \rightarrow 5 + 15 * 20 - 7$**



Prediktivno parsiranje

- LL(k) parser - s lijeva na desno, najljeviji izvod, k-simbola lookahead
 - Odluka o odabiru produkcije gramatike donosi se na temelju provjere narednih k tokena
 - LL(k) gramatika – gramatika koju je moguće parsirati LL(k) parserom
- LL(1) parser – produkcija gramatike se bira samo na temelju idućeg tokena

Gramatika:

$$\begin{aligned} E &::= E + T \mid E - T \mid T \\ T &::= T * F \mid T / F \mid F \\ F &::= n \end{aligned}$$

**Svaka produkcija za E
započinje s E -> nije LL(K)**

Ekvivalentna LL(1) gramatika :

Gramatika:

$$\begin{aligned} E &::= TE' \\ E' &::= + TE' \mid - TE' \mid \varepsilon \\ T &::= FT' \\ T' &::= *FT' \mid / FT' \mid \varepsilon \\ F &::= n \end{aligned}$$

LL(1) parsiranje - Primjer

Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

$() \$$

- \$ - oznaka dna stoga i kraja ulazne riječi

\$

LL(1) parsiranje - Primjer

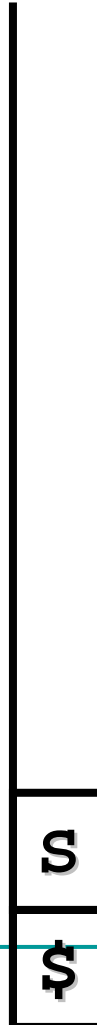
Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

$() \$$

- Stavimo početni simbol S na stog



LL(1) parsiranje - Primjer

Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

$() \$$

- Expand: $S \rightarrow (S) S$



LL(1) parsiranje - Primjer

Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

$() \$$

■ Match



LL(1) parsiranje - Primjer

Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

)\$

- Expand: $S \rightarrow \epsilon$



LL(1) parsiranje - Primjer

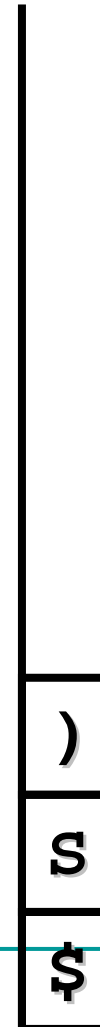
Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

)\$

- Expand: $S \rightarrow \epsilon$



LL(1) parsiranje - Primjer

Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

)\$

■ Match



LL(1) parsiranje - Primjer

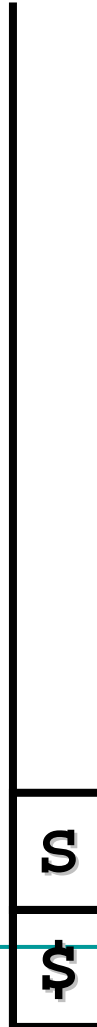
Gramatika

$S \rightarrow (S) S \mid \varepsilon$

Ulaz

\$

- Expand: $S \rightarrow \varepsilon$



LL(1) parsiranje - Primjer

Gramatika

$S \rightarrow (S) S \mid \varepsilon$

Ulaz

\$

- Expand: $S \rightarrow \varepsilon$

\$

LL(1) parsiranje - Primjer

Gramatika

$S \rightarrow (S) S \mid \epsilon$

Ulaz

\$

- Parsiranje uspješno završilo!

\$

Bottom-up parsiranje

- Počevši od ulaznog stringa, trebamo reducirati ulazni string na početni neterminalni simbol (ekvivalentno obrnutom najdesnijem izvodu)

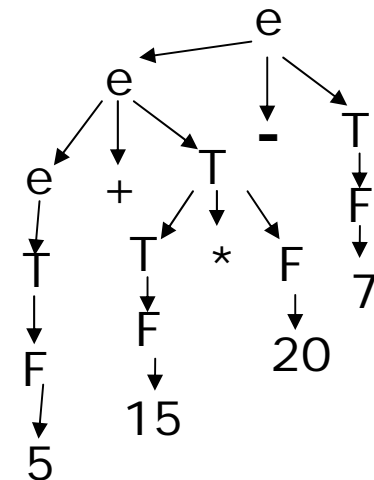
Gramatika:

$$\begin{aligned} E &::= E + T \mid E - T \mid T \\ T &::= T * F \mid T / F \mid F \\ F &::= n \end{aligned}$$

Najdesniji izvod za $5+15*20-7$:

$$\begin{aligned} E &\rightarrow E - T \rightarrow E - F \rightarrow E - 7 \rightarrow E + T - 7 \rightarrow E + T * F - 7 \\ &\rightarrow E + T * 20 - 7 \rightarrow E + F * 20 - 7 \rightarrow E + 15 * 20 - 7 \\ &\rightarrow T + 15 * 20 - 7 \rightarrow F + 15 * 20 - 7 \rightarrow 5 + 15 * 20 - 7 \end{aligned}$$

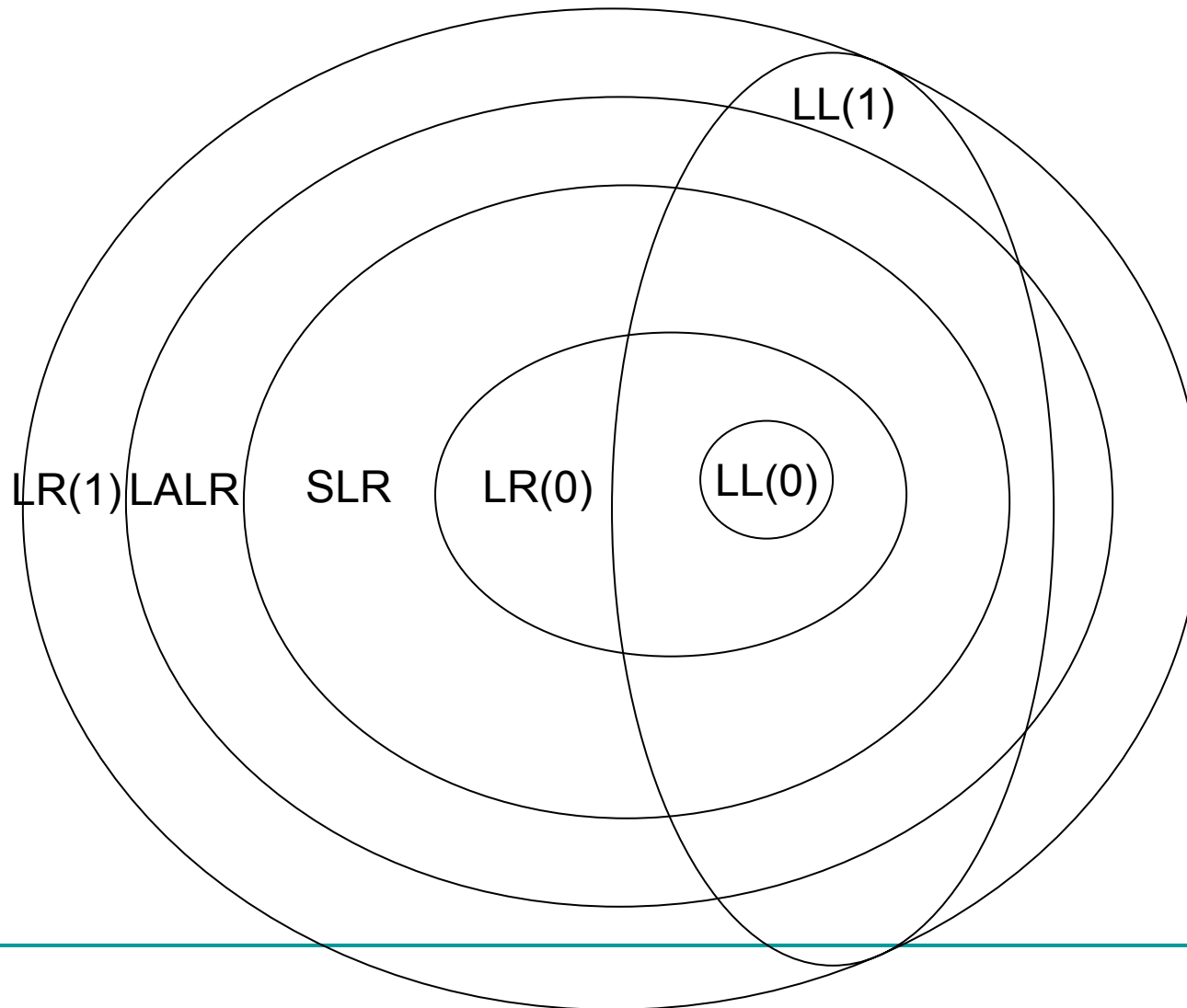
Bottom-up parsiranje:

$$\begin{aligned} 5 + 15 * 20 - 7 &\rightarrow F + 15 * 20 - 7 \rightarrow T + 15 * 20 - 7 \\ &\rightarrow E + 15 * 20 - 7 \rightarrow E + F * 20 - 7 \rightarrow E + T * 20 - 7 \\ &\rightarrow E + T * F - 7 \rightarrow E + T - 7 \rightarrow E - 7 \rightarrow E - F \rightarrow E - T \rightarrow E \end{aligned}$$


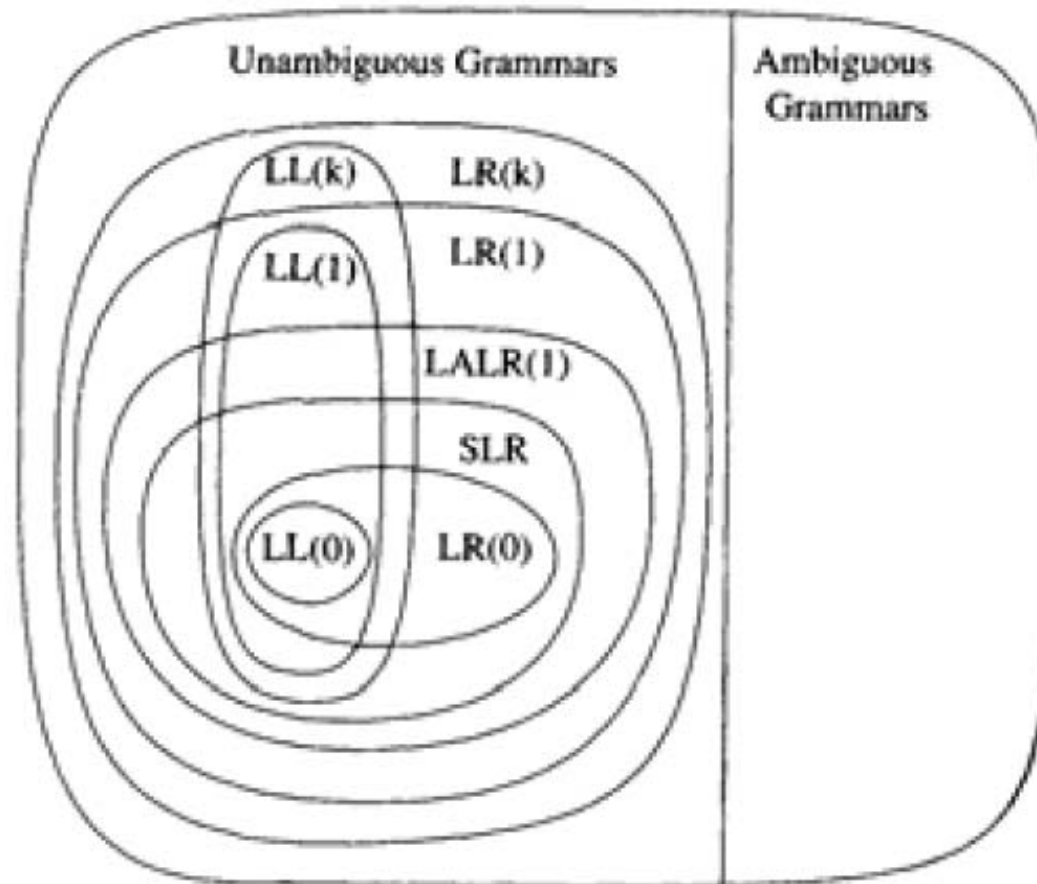
LR(k) parsiranje

- LR(k) parser - s lijeva na desno, najdesniji izvod, k simbola lookahead
 - Odluke donose na temelju provjere narednih k tokena
 - Koriste konačne automate za konfiguraciju akcija (shift ili reduce)
 - Stanja automata pamte simbole koji su već na stogu
 - Svaki par (stanje, token) jedinstveno određuje iduću akciju
 - Zašto koristiti LR parsere?
 - Prepoznaju širu klasu KS jezika od prediktivnih LL(k) parsera
 - Efikasna implementacija, nema backtrackinga
 - LR(k) vs LL(k):
 - LL parseri – pogodni za "ručnu" implementaciju (jednostavan programski kod)
 - LR parseri – bitno teža "ručna" implementacija; obično se koriste automatski generatori (npr. Yacc/Bison) -> kompliciran i "ružan" programski kod
-

Odnos među klasama gramatika

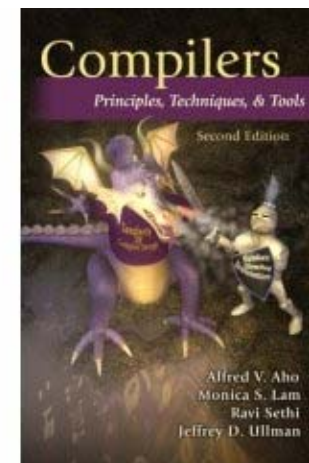
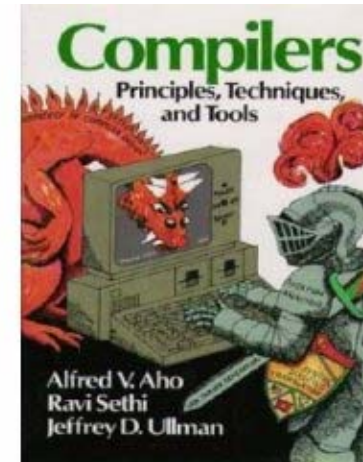


Odnos među klasama gramatika



The Dragon Book

- **Compilers: Principles, Techniques and Tools**
 - Alfred V. Aho, Ravi Sethi, Jeffrey D. Ullman (1st Edition)
 - Alfred V. Aho, Monica S. Lam, Ravi Sethi, Jeffrey D. Ullman (2nd Edition)



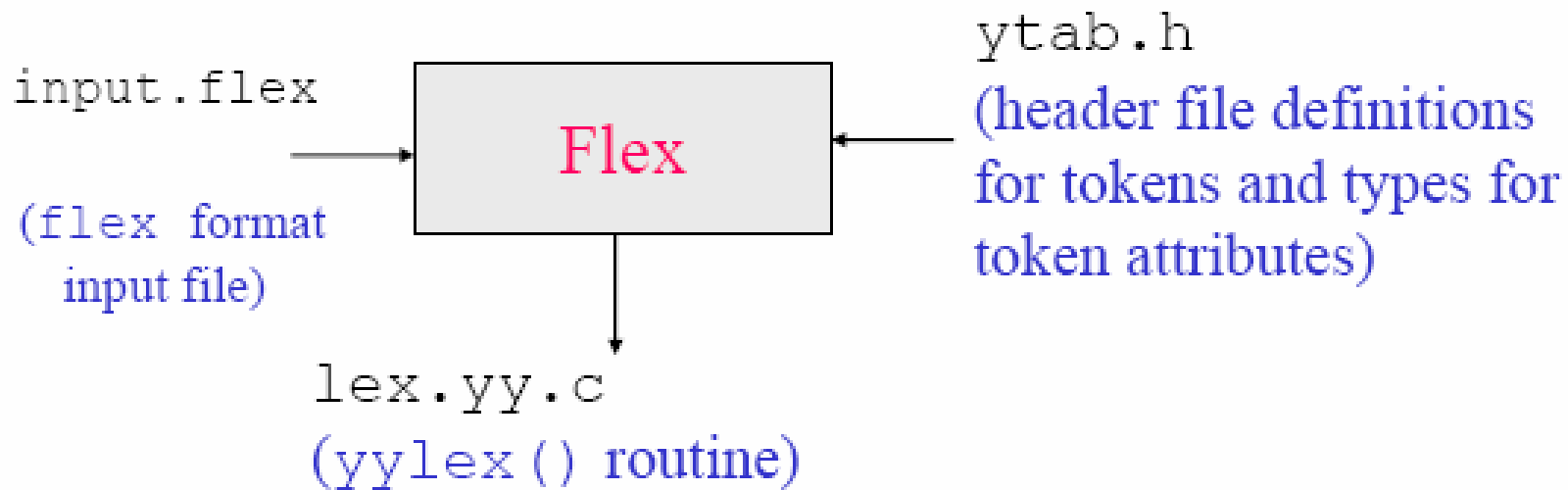


Alati za generiranje lexera / parsera

(F)lex

- (F)lex = (Fast) Lexical Analyzer Generator
 - Neke implementacije:
 - Flex for Windows
 - <http://gnuwin32.sourceforge.net/packages/flex.htm>
 - JFlex
 - <http://www.jflex.de/>
-

(F)lex



definitions

%%

rules

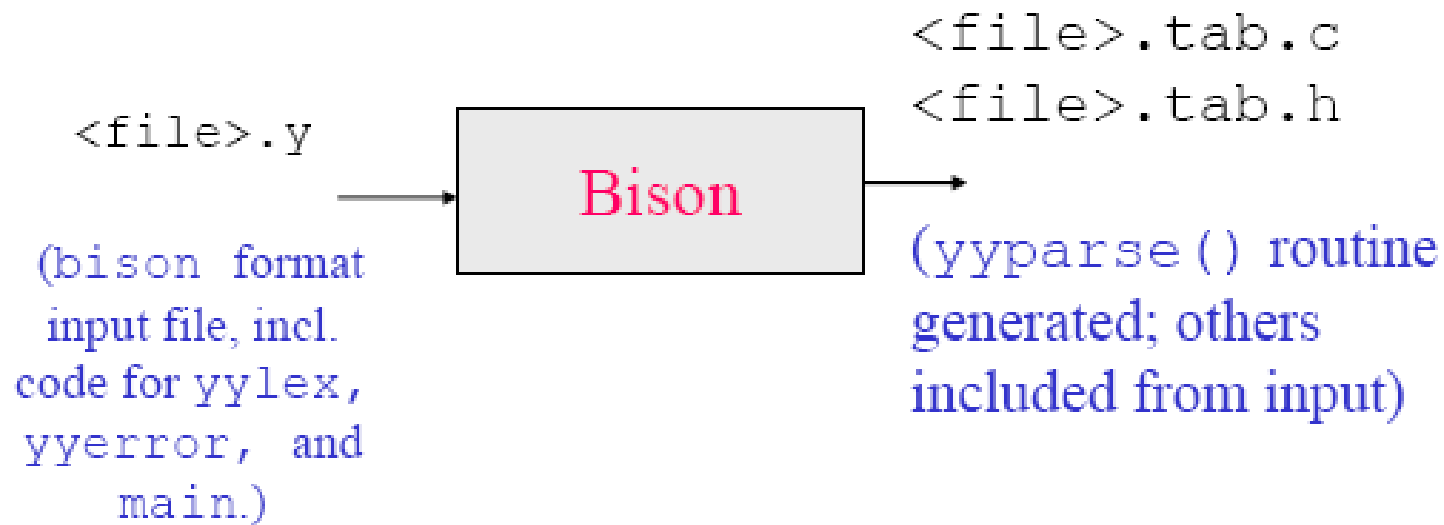
%%

user code

Yacc/Bison

- Yacc = Yet Another Compiler-Compiler
 - generator LALR(1) parsera
 - Bison – generator LALR(1) / GLR parsera (kompatibilan s Yacc-ovom sintaksom ulaza)
 - Neke implementacije:
 - Bison for Windows
 - <http://gnuwin32.sourceforge.net/packages/bison.htm>
 - BYACC/J
 - <http://byaccj.sourceforge.net/>
-

Yacc/Bison



Yacc/Bison

The input file consists of three sections, separated by a line with just `'%%'` on it:

```
%{
```

```
C declarations (types, variables, functions,  
preprocessor commands)
```

```
%}
```

```
Bison declarations (grammar symbols,  
operator precedence decl.,  
attribute data type)
```

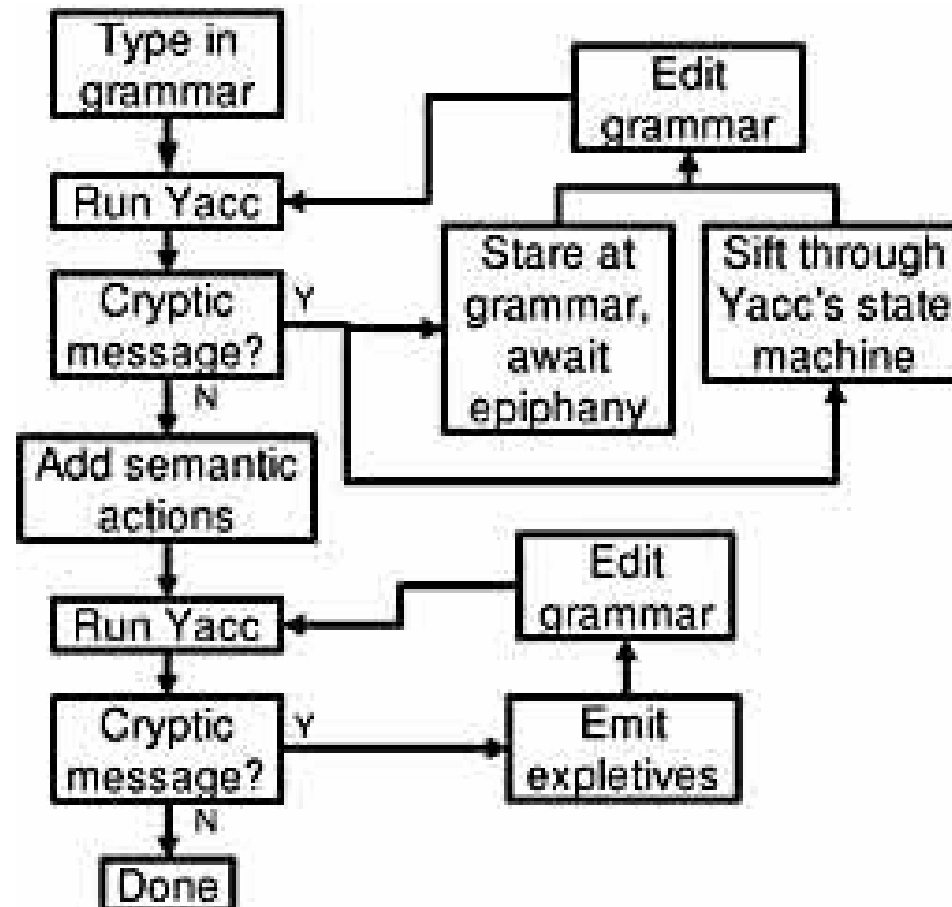
```
%%
```

```
Grammar rules
```

```
%%
```

```
Additional C code (incl. scanner yylex)
```

Ciklus razvoja parsera s Yacc/Bison-om



<http://www.acm.org/crossroads/xrds7-5/bison.html>

ANTLR

- ANTLR = ANoTher Tool for Language Recognition
 - generator lexera i LL(k) parsera
 - zapravo LL(*) s linearnom aproksimacijom lookaheada i sintaktičkim/semantičkim predikatima
 - zajednička sintaksa za specifikaciju lexera i parsera
 - Linkovi:
 - ANTLR
 - <http://www.antlr.org/>
 - ANTLR plugin za Eclipse
 - <http://antreclipse.sourceforge.net/>
-