

# Asocijacijske sheme

Vedran Krčadinac

20.11.2023.

G. Chen, I. Ponomarenko, *Lectures on coherent configurations*, 2018.

<http://www.pdmi.ras.ru/~inp/ccNOTES.pdf>

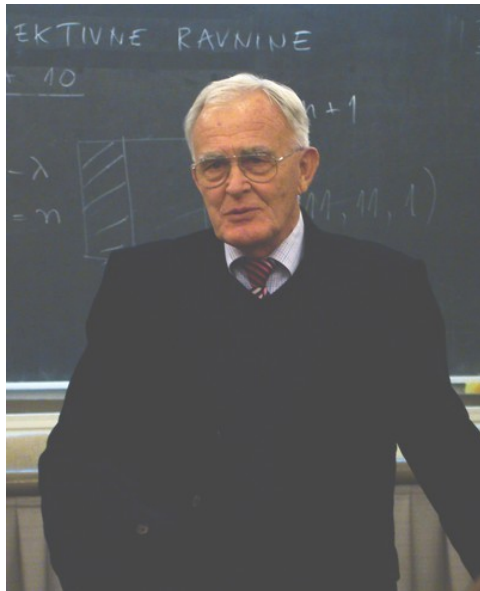
G. Chen, I. Ponomarenko, *Lectures on coherent configurations*, 2018.

<http://www.pdmi.ras.ru/~inp/ccNOTES.pdf>

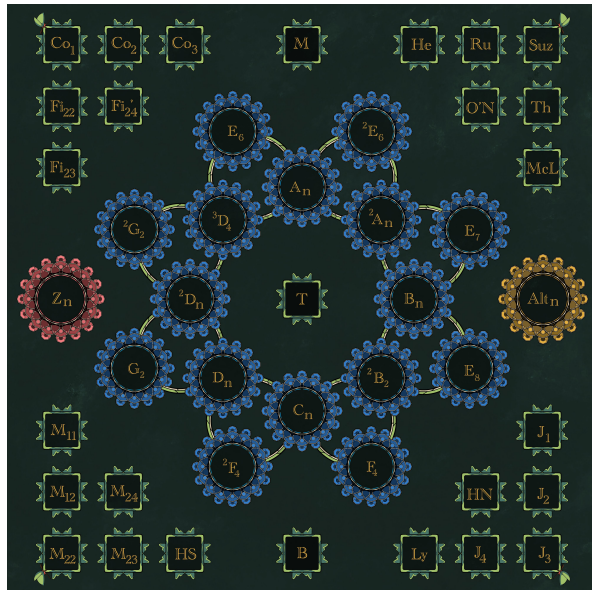
Paul Terwilliger, *Math 846 – Algebraic Combinatorics: Association Schemes*, 2023.

<https://people.math.wisc.edu/~pfterwil/>

# Prof. Zvonimir Janko (1932.-2022.)



# Klasifikacija konačnih jednostavnih grupa



Z. Janko, *A new finite simple group with abelian Sylow 2-subgroups and its characterization*, J. Algebra **3** (1966), 147–186.

Z. Janko, *A new finite simple group with abelian Sylow 2-subgroups and its characterization*, J. Algebra **3** (1966), 147–186.  $\rightsquigarrow |J_1| = 175\,560$

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R. L. Griess, Jr., *The structure of the “monster” simple group*, Proceedings of the Conference on Finite Groups (Univ. Utah, 1975), pp. 113–118.

Z. Janko, *A new finite simple group with abelian Sylow 2-subgroups and its characterization*, J. Algebra **3** (1966), 147–186.  $\rightsquigarrow |J_1| = 175\,560$

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R. L. Griess, Jr., *The structure of the “monster” simple group*, Proceedings of the Conference on Finite Groups (Univ. Utah, 1975), pp. 113–118.

$\rightsquigarrow |M| = 808\,017\,424\,794\,512\,875\,886\,459\,904\,961\,710\,757\,005\,754\,368\,000\,000\,000$

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Z. Janko, *A new finite simple group of order 86 775 571 046 077 562 880 which possesses  $M_{24}$  and the full covering group of  $M_{22}$  as subgroups*, J. Algebra **42** (1976), no. 2, 564–596.

Z. Janko, *A new finite simple group with abelian Sylow 2-subgroups and its characterization*, J. Algebra **3** (1966), 147–186.  $\rightsquigarrow |J_1| = 175\,560$

D. G. Higman, C. C. Sims, *A simple group of order 44 352 000*, Math. Z. **105** (1968), 110–113.  $\rightsquigarrow HS$

R. L. Griess, Jr., *The structure of the “monster” simple group*, Proceedings of the Conference on Finite Groups (Univ. Utah, 1975), pp. 113–118.

$\rightsquigarrow |M| = 808\,017\,424\,794\,512\,875\,886\,459\,904\,961\,710\,757\,005\,754\,368\,000\,000\,000$

Z. Janko, *A new finite simple group of order 86 775 571 046 077 562 880 which possesses  $M_{24}$  and the full covering group of  $M_{22}$  as subgroups*, J. Algebra **42** (1976), no. 2, 564–596.  $\rightsquigarrow J_4$

# Konstrukcije simetričnih dizajna

Z. Janko, T. V. Tran, *The existence of a symmetric block design for  $(70, 24, 8)$* , Mitt. Math. Sem. Giessen No. **165** (1984), 17–18.

Z. Janko, T. V. Tran, *The existence of a symmetric block design for  $(70, 24, 8)$* , Mitt. Math. Sem. Giessen No. **165** (1984), 17–18.

Z. Janko, T. V. Tran, *Construction of two symmetric block designs for  $(71, 21, 6)$* , Discrete Math. **55** (1985), no. 3, 327–328.



Z. Janko, T. V. Tran, *The existence of a symmetric block design for  $(70, 24, 8)$* , Mitt. Math. Sem. Giessen No. **165** (1984), 17–18.

Z. Janko, T. V. Tran, *Construction of two symmetric block designs for  $(71, 21, 6)$* , Discrete Math. **55** (1985), no. 3, 327–328.

Z. Janko, T. V. Tran, *Construction of a new symmetric block design for  $(78, 22, 6)$  with the help of tactical decompositions*, J. Combin. Theory Ser. A, **40** (1985), 451–455.

Z. Janko, T. V. Tran, *The existence of a symmetric block design for  $(70, 24, 8)$* , Mitt. Math. Sem. Giessen No. **165** (1984), 17–18.

Z. Janko, T. V. Tran, *Construction of two symmetric block designs for  $(71, 21, 6)$* , Discrete Math. **55** (1985), no. 3, 327–328.

Z. Janko, T. V. Tran, *Construction of a new symmetric block design for  $(78, 22, 6)$  with the help of tactical decompositions*, J. Combin. Theory Ser. A, **40** (1985), 451–455.

Z. Janko, *The existence of symmetric designs with parameters  $(189, 48, 12)$* , J. Combin. Theory Ser. A **80** (1997), no. 2, 334–338.

Z. Janko, T. V. Tran, *The existence of a symmetric block design for  $(70, 24, 8)$* , Mitt. Math. Sem. Giessen No. **165** (1984), 17–18.

Z. Janko, T. V. Tran, *Construction of two symmetric block designs for  $(71, 21, 6)$* , Discrete Math. **55** (1985), no. 3, 327–328.

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Z. Janko, *The existence of symmetric designs with parameters  $(189, 48, 12)$* , J. Combin. Theory Ser. A **80** (1997), no. 2, 334–338.

Z. Janko, *The existence of symmetric designs with parameters  $(105, 40, 15)$* , J. Combin. Des. **7** (1999), no. 1, 17–19.

Z. Janko, *The existence of a Bush-type Hadamard matrix of order 36 and two new infinite classes of symmetric designs*, J. Combin. Theory Ser. A **95** (2001), no. 2, 360–364.

Z. Janko, H. Kharaghani, V. D. Tonchev, *The existence of a Bush-type Hadamard matrix of order 324 and two new infinite classes of symmetric designs*, Des. Codes Cryptogr. **24** (2001), no. 2, 225–232.

Z. Janko, *The existence of a Bush-type Hadamard matrix of order 36 and two new infinite classes of symmetric designs*, J. Combin. Theory Ser. A **95** (2001), no. 2, 360–364.

Z. Janko, H. Kharaghani, V. D. Tonchev, *The existence of a Bush-type Hadamard matrix of order 324 and two new infinite classes of symmetric designs*, Des. Codes Cryptogr. **24** (2001), no. 2, 225–232.

Z. Janko, H. Kharaghani, *A block negacyclic Bush-type Hadamard matrix and two strongly regular graphs*, J. Combin. Theory Ser. A **98** (2002), no. 1, 118–126.

Z. Janko, *The existence of a Bush-type Hadamard matrix of order 36 and two new infinite classes of symmetric designs*, J. Combin. Theory Ser. A **95** (2001), no. 2, 360–364.

Z. Janko, H. Kharaghani, V. D. Tonchev, *The existence of a Bush-type Hadamard matrix of order 324 and two new infinite classes of symmetric designs*, Des. Codes Cryptogr. **24** (2001), no. 2, 225–232.

Z. Janko, H. Kharaghani, *A block negacyclic Bush-type Hadamard matrix and two strongly regular graphs*, J. Combin. Theory Ser. A **98** (2002), no. 1, 118–126.  $\rightsquigarrow$   $SRG(936, 375, 150, 150)$ ,  $SRG(1800, 1029, 588, 588)$

Y. Berkovich, *Groups of prime power order, Vol. 1*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008.

Y. Berkovich, *Groups of prime power order, Vol. 1*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008. (with a foreword by Z. Janko)



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Y. Berkovich, Z. Janko, *Groups of prime power order, Vol. 2*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008.

Y. Berkovich, *Groups of prime power order, Vol. 1*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008. (with a foreword by Z. Janko)

Y. Berkovich, Z. Janko, *Groups of prime power order, Vol. 2*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008.

Volume 3, 2011.

Y. Berkovich, *Groups of prime power order, Vol. 1*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008. (with a foreword by Z. Janko)

Y. Berkovich, Z. Janko, *Groups of prime power order, Vol. 2*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008.

Volume 3, 2011.

Volume 4, 2016.

Y. Berkovich, *Groups of prime power order, Vol. 1*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008. (with a foreword by Z. Janko)

Y. Berkovich, Z. Janko, *Groups of prime power order, Vol. 2*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008.

Volume 3, 2011.

Volume 4, 2016.

Volume 5, 2016.

Y. Berkovich, *Groups of prime power order, Vol. 1*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008. (with a foreword by Z. Janko)

Y. Berkovich, Z. Janko, *Groups of prime power order, Vol. 2*, Walter de Gruyter GmbH & Co. KG, Berlin, 2008.

Volume 3, 2011.

Volume 4, 2016.

Volume 5, 2016.

Volume 6, 2018.

# Primjer 1.37

$$[p_{ij}^0] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}, \quad [p_{ij}^1] = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad [p_{ij}^2] = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

# Primjer 1.39

$$[p_{ij}^0] = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}, \quad [p_{ij}^1] = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix},$$

$$[p_{ij}^2] = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix}, \quad [p_{ij}^3] = \begin{bmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix},$$

# Primjer 1.39

$$[p_{ij}^4] = \begin{bmatrix} 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \end{bmatrix}, \quad [p_{ij}^5] = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$