

# Asocijacijske sheme

Vedran Krčadinac

2023./24.

# Kratka povijest asocijacijskih shema

- **Asocijacijske sheme** (statističari, 1950-e)

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R. C. Bose, T. Shimamoto, *Classification and analysis of partially balanced incomplete block designs with two associate classes*, J. Amer. Statist. Assoc. **47** (1952), 151–184.

R. C. Bose, D. M. Mesner, *On linear associative algebras corresponding to association schemes of partially balanced designs*, Ann. Math. Statist. **30** (1959), 21–38.

S. S. Shrikhande, *The uniqueness of the  $L_2$  association scheme*, Ann. Math. Statist. **30** (1959), 781–798.

## Raj Chandra Bose

From Wikipedia, the free encyclopedia

**Raj Chandra Bose** (19 June 1901 – 31 October 1987) was an **Indian American** mathematician and statistician best known for his work in **design theory**, **finite geometry** and the theory of **error-correcting codes** in which the class of **BCH codes** is partly named after him. He also invented the notions of **partial geometry**, **association scheme**, and **strongly regular graph** and started a systematic study of **difference sets** to construct symmetric **block designs**. He was notable for his work along with **S. S. Shrikhande** and **E. T. Parker** in their disproof of the famous **conjecture** made by **Leonhard Euler** dated 1782 that there do not exist two mutually orthogonal **Latin squares** of order  $4n + 2$  for every  $n$ .

**Raj Chandra Bose**



Izvor: [https://en.wikipedia.org/wiki/Raj\\_Chandra\\_Bose](https://en.wikipedia.org/wiki/Raj_Chandra_Bose)

## Dale Marsh Mesner



April 13, 1923 ~  
December 8, 2009

Resided in: **Pueblo, CO**

Dale Marsh Mesner, Professor of Mathematics. Dale first opened his eyes in a Nebraska farmhouse in 1923. Dale disliked farm work but loved numbers, read the entire dictionary and encyclopedia and won the Nebraska state spelling bee. In WWII, Dale, a Quaker, enlisted as a medic. He served in, of all places, Brazil, where he took X-rays of soldiers mustering out of the European war. Dale earned his PhD in mathematics from Michigan State University in 1956. Math was his deepest passion. He worked on the earliest computers, ones that filled an entire floor of a building. He did ground breaking research (google Bose-Mesner Algebra.) Dale taught at the University of Nebraska where he retired Professor Emeritus in 1990. He walked, talked, dreamt and researched mathematics until his final days. Dale also loved music and literature. He cared deeply for humanity and hated injustice. In 1948, he met and married Marian Woolcock, daughter of a Michigan auto worker. They served as Christian missionaries in Cuba, then raised a family stateside. He marched for Civil Rights and against the KKK in the 1960's. He opposed wars and nuclear weapons. He organized for the rights of Gays and Lesbians and in the 80's escorted women to Family Planning Clinics. All these concerns and loves he passed on to his children, Doug (Diane), Nancy (Chris Luecke), Mary (Terry Werner), Paul (David Luckens), Eric and foster son, Richard Stark. Dale has nine wonderful grandchildren. In 2008, Dale bravely survived massive cancer surgery and treatments. He and Marian moved to Pueblo in July 2009. He took good care of Marian who also has health problems. Three weeks ago he fell and broke four ribs. He closed his eyes December 8. Services will be 11 a.m. Monday, December 21, 2009, at the Unitarian Church in Lincoln, Neb. Online condolences, [www.montgomerysteward.com](http://www.montgomerysteward.com)

Izvor: <https://www.montgomerysteward.com/obits/dale-marsh-mesner/>

## Obituary: S.S. Shrikhande, 1917–2020

MAY 17, 2020



*Shartchandra Shankar Shrikhande*

Shartchandra Shankar Shrikhande, IMS Fellow and well known combinatorial mathematician, passed away on April 21 at his residence in India. He was 102.

S.S. Shrikhande was born in Sagar, India, on October 19, 1917. Having won scholarships, he was able to complete his BSc Honours at the Government College of Science (now known as the Institute of Science) in Nagpur with a first rank and a gold medal. He went on to receive his doctoral degree on Construction of Partially Balanced Designs from the University of North Carolina in 1950, under the supervision of Raj Chandra Bose. Prior to that, he was a Research Fellow at the

Indian Statistical Institute. Professor Shrikhande, R.C. Bose and E. T. Parker jointly disproved Euler's 1782 conjecture that mutually orthogonal Latin squares cannot exist for orders of the form  $4n+2$  for any  $n$ . This was proved by Euler himself for  $n=0$  and by Gaston Tarry in 1901 for  $n=1$ . The first analytical counterexample was found by Bose and Shrikhande in early 1959 for  $n=5$ . Later the same year, Bose, Shrikhande and Parker proved the general result that in fact such orthogonal squares exist for all orders  $4n+2$  except  $n=0,1$ . The trio were dubbed "Euler's Spoilers"—as reported in the front-page New York Times article on April 26, 1959.

Izvor: <https://imstat.org/2020/05/17/obituary-s-s-shrikhande-1917-2020/>





- **Koherentne kofiguracije** (istraživanja permutacijskih grupa, 1970-e)

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D. G. Higman, *Coherent configurations. I. Ordinary representation theory*, Geometriae Dedicata **4** (1975), no. 1, 1–32.

D. G. Higman, *Coherent configurations. II. Weights*, Geometriae Dedicata **5** (1976), no. 4, 413–424.

P. J. Cameron, *Suborbits in transitive permutation groups*, Combinatorics (Proc. NATO Advanced Study Inst., Breukelen, 1974), Part 3: Combinatorial group theory, pp. 98–129, Math. Centre Tracts, No. 57, Mathematisch Centrum, Amsterdam, 1974.

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↪ “Teorija grupa bez grupa”

## ☰ Donald G. Higman

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From Wikipedia, the free encyclopedia

*Not to be confused with [Graham Higman](#).*

**Donald G. Higman** (September 20, 1928 in [Vancouver](#) – February 13, 2006) was an [American mathematician](#) known for his discovery, in collaboration with [Charles C. Sims](#), of the [Higman–Sims group](#).<sup>[1]</sup>

Higman did his undergraduate studies at the [University of British Columbia](#),<sup>[1]</sup> and received his Ph.D. in 1952 from the [University of Illinois Urbana-Champaign](#) under [Reinhold Baer](#).<sup>[2]</sup> He served on the faculty of mathematics at the [University of Michigan](#) from 1956 to 1998.<sup>[1]</sup>

His work on homological aspects of group [representation theory](#) established the concept of a relatively [projective module](#) and explained its role in the theory of module decompositions. He developed a characterization of rank-2 [permutation groups](#), and a theory of rank-3 permutation groups; several of the later-discovered [sporadic simple groups](#) were of this type, including the Higman–Sims group which he and Sims constructed in 1967.<sup>[1]</sup>

Izvor: [https://en.wikipedia.org/wiki/Donald\\_G.\\_Higman](https://en.wikipedia.org/wiki/Donald_G._Higman)

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Izvor: [https://en.wikipedia.org/wiki/Donald\\_G.\\_Higman](https://en.wikipedia.org/wiki/Donald_G._Higman)

E. Bannai, R. L. Griess Jr., C. E. Praeger, L. Scott, *The mathematics of Donald Gordon Higman*, Michigan Math. J. **58** (2009), no. 1, 3–30.

## Graham Higman

From Wikipedia, the free encyclopedia

*Not to be confused with [Donald G. Higman](#).*

**Graham Higman** FRS<sup>[1]</sup> (19 January 1917 – 8 April 2008) was a prominent English **mathematician** known for his contributions to **group theory**.

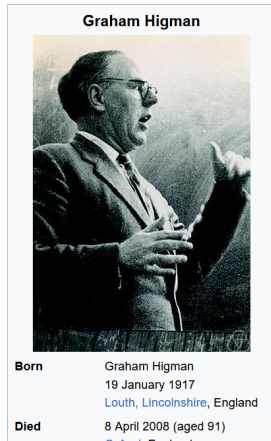
### Biography [edit]

Higman was born in **Louth, Lincolnshire**, and attended Sutton High School, **Plymouth**, winning a scholarship to **Balliol College, Oxford**.<sup>[2]</sup> In 1939 he co-founded **The Invariant Society**, the student mathematics society,<sup>[3]</sup> and earned his DPhil from the **University of Oxford** in 1941. His thesis, *The units of group-rings*, was written under the direction of **J. H. C. Whitehead**. From 1960 to 1984 he was the **Waynflete Professor of Pure Mathematics** at **Magdalen College, Oxford**.

Higman was awarded the **Senior Berwick Prize** in 1962 and the **De Morgan Medal** of the **London Mathematical Society** in 1974. He was the founder of the **Journal of Algebra** and its editor from 1964 to 1984. Higman had 51 D.Phil. students, including **Jonathan Lazare Alperin**, **Rosemary A. Bailey**, **Marston Conder**, **John Mackintosh Howie**, and **Peter M. Neumann**.

He was also a **local preacher** in the Oxford Circuit of the **Methodist Church**. During the **Second World War** he was a **conscientious objector**, working at the **Meteorological Office** in **Northern Ireland** and **Gibraltar**.

He died in Oxford.<sup>[2]</sup>



Izvor: [https://en.wikipedia.org/wiki/Graham\\_Higman](https://en.wikipedia.org/wiki/Graham_Higman)

- **Celularni prsteni** (sovjetski matematičari, 1970-e)

- **Celularni prsteni** (sovjetski matematičari, 1970-e)

B. Weisfeiler, A. A. Leman, *Reduction of a graph to a canonical form and an algebra which appears in this process*, Scientific-Technological Investigations **2** (1968), 12–16.

I. A. Faradžev, M. H. Klin, M. E. Muzichuk, *Cellular rings and groups of automorphisms of graphs*, Investigations in algebraic theory of combinatorial objects, 1–152, Math. Appl. (Soviet Ser.), 84, Kluwer Acad. Publ., 1994.



## Boris Weisfeiler

From Wikipedia, the free encyclopedia

**Boris Weisfeiler** (born 19 April 1941 – disappeared 4–5 January 1985)<sup>[1]</sup> was a [Soviet](#)-born mathematician and professor at [Penn State University](#) who lived in the United States before disappearing in [Chile](#) in 1985. Declassified US documents suggest a Chilean army patrol seized Weisfeiler and took him to [Colonia Dignidad](#), a secretive Germanic agricultural commune set up in Chile in the 1960s.<sup>[2]</sup> During the Chilean [Pinochet military dictatorship](#) Boris Weisfeiler allegedly drowned. He is known for the Weisfeiler filtration, [Weisfeiler–Leman algorithm](#) and [Kac–Weisfeiler conjectures](#).

### Early life and career [[edit](#)]

Weisfeiler, a [Jew](#), was born in the [Soviet Union](#). He received his [Ph.D.](#) in 1970 from the [Steklov Institute of Mathematics Leningrad](#) Department, as a student of [Ernest Vinberg](#).<sup>[3]</sup> In the early 1970s, Weisfeiler was asked to sign a letter against a colleague, and for his refusal was branded "anti-Soviet". Weisfeiler left the Soviet Union in 1975 to be free to advance his career and practice his religion. After a brief period under [Armand Borel](#) at the [Institute for Advanced Study](#), near [Princeton University](#), Weisfeiler became a professor at [Pennsylvania State University](#). In 1981, he was [naturalized](#) as an [American citizen](#).

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<b>Boris Yulievich Weisfeiler</b>	
<b>Born</b>	April 19, 1941 <div>Moscow, Russian SFSR, Soviet Union</div>
<b>Disappeared</b>	January 1985 <div>San Fabián de Alico, Chile</div>
<b>Status</b>	Missing for 38 years, 9 months and 30 days
<b>Nationality</b>	American
<b>Alma mater</b>	Steklov Institute of Mathematics (Ph.D.)
<b>Known for</b>	Weisfeiler–Leman algorithm Weisfeiler filtration Kac–Weisfeiler conjectures
<b>Scientific career</b>	
<b>Fields</b>	Mathematics
<b>Institutions</b>	<a href="#">Pennsylvania State University</a>
<b>Institutions</b>	<a href="#">Pennsylvania State University</a>

Izvor: [https://en.wikipedia.org/wiki/Boris\\_Weisfeiler](https://en.wikipedia.org/wiki/Boris_Weisfeiler)

# Kratka povijest asocijacijskih shema



## MISSING IN CHILE



**MATHEMATICS PROFESSOR  
BORIS WEISFEILER  
HAS BEEN MISSING IN  
CHILE SINCE  
JANUARY 4, 1985**



### DID YOU SEE THIS MAN?



### ¿Ha visto a este hombre? Did you see this man?

With information please contact:  
Brigada Investigadora de Asuntos  
Especiales y de Derechos Humanos  
(56-2) 3657475 or the FBI Attaché at  
the U.S. Embassy in Santiago, Chile at  
(56-2) 330-3396

### ABOUT BORIS

**Boris Weisfeiler: la obra  
impredecible del matemático  
desaparecido en Chile en 1985**  
El Mostrador, March 30, 2016

### SEARCHING FOR BORIS WEISFEILER: SEQUENCE OF EVENTS

#### 2023. THE SUPREME COURT TO HEAR THE ARGUMENTS

On May 4, 2023, more than 3 years after our appeal was filed, the Second Chamber of the Supreme Court heard Boris's case. Hernan Fernandez, the Weisfeiler family's attorney, Joaquin Perera from the Human Rights Program, and Ricardo Gonzales from the State Defense Council made their cases before the Second Chamber. Joaquín Perera presented his arguments first, followed by Hernán Fernandez, and Ricardo González closed.

On the second day of the hearing on May 5, two defense attorneys representing military members involved in Boris's kidnapping and disappearance presented their arguments. No defense attorney represented the four Carabineros involved in the case.

It could take months before the Court's decision will be announced.

### LATEST DEVELOPMENTS

**The Supreme Court to hear the arguments**  
YouTube, May 4-5, 2023, Santiago, Chile (in Spanish)

**U.S. Ambassador to Chile Bernadette Meehan's Zoom meeting with Olga Weisfeiler**  
Chile-US, March 10, 2023

The book **Boris, 1985** by Douna Loop  
France, January 2023  
Available for purchase [here](#) (in French)  
The book sample [translated into English](#)

**Commemorating 80th birthday of Boris Weisfeiler / Conmemoración 80 años Boris Weisfeiler**  
YouTube, April 19, 2021, Santiago, Chile  
(in English and Spanish)  
Speakers: Attorney Hernan Fernandez, Olga Weisfeiler, Math Prof. Andres Navas, Martin Grohe, Igor Dolgachev

**A short video/Testimonial/ Olga Weisfeiler**  
Vimeo.com /by Marella Oppenheim, October 13, 2019

**Excavations at Chile torture site offer new hope for relatives of disappeared**  
The Guardian, US, May 2, 2018

**Missing in Chile: What happened to Boris Weisfeiler?**  
BBC, April 10, 2016

**Chile Halts Inquiry on American Who Disappeared 31 Years Ago**  
The New York Times, March 10, 2016

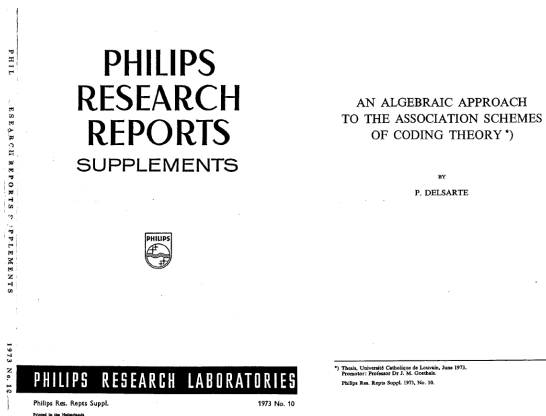
Izvor: <http://boris.weisfeiler.com/>

- **Disertacija Philippe Delsartea (1973.)**

P. Delsarte, *An algebraic approach to the association schemes of coding theory*, Philips Res. Rep. Suppl. 1973, no. 10, vi+97 pp.

- **Disertacija Philippe Delsartea (1973.)**

P. Delsarte, *An algebraic approach to the association schemes of coding theory*, Philips Res. Rep. Suppl. 1973, no. 10, vi+97 pp.



- **Knjige**

E. Bannai, T. Ito, *Algebraic combinatorics. I. Association schemes*, The Benjamin/Cummings Publishing Co., 1984.

A. E. Brouwer, A. M. Cohen, A. Neumaier, *Distance-regular graphs*, Springer-Verlag, 1989.

C. D. Godsil, *Algebraic combinatorics*, Chapman & Hall, 1993.

R. A. Bailey, *Association schemes. Designed experiments, algebra and combinatorics*, Cambridge University Press, 2004.

E. Bannai, E. Bannai, T. Ito, R. Tanaka, *Algebraic combinatorics*, De Gruyter, 2021.

# Što je asocijacijska shema?

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Definicion. A SEMIRING ( $S$ -ring)  
over a group ring  $\mathbb{Z}(H)$  is a subring  $\mathcal{T}$   
of the group ring  $\mathbb{Z}(H)$  such  
that there exist subsets  $T_0, T_1, \dots,$   
 $T_d$  of  $H$  satisfying the following  
properties:

- (1)  $\mathcal{T}$  has a  $\mathbb{Z}$ -module basis of  
simple quantities:  $\mathcal{T} = \langle T_0, T_1, \dots, T_d \rangle$ ,
- (2)  $T_0 = \{0\}$  and  $\bigcup_{i=0}^d T_i = H$ , that is  
 $\{T_0, T_1, \dots, T_d\}$  is a partition  
of  $H$ ,
- (3)  $\forall i \exists j \ T_i^T = T_j$ , where  
 $T_i^T = \{-x \mid x \in T_i\}$ .

# Što je asocijacijska shema?

## Algebraic Coding Theory-Honoring the Retirement of Vera Pless

At 2006 Fall Central Section Meeting, Cincinnati, OH, October 21-22, 2006

Group Photos (a), (b)



Group Photo 1

[Tsvetan I. Asamov 1](#), [Tsvetan I. Asamov 2](#),

[Alexander Barg 1](#), [Alexander Barg 2](#),

[Steven T. Dougherty 1](#), [Steven T. Dougherty 2](#),

[Iwan M. Duursma 1](#), [Iwan M. Duursma 2](#),

[Philippe Gaborit](#),

[T. Aaron Gulliver 1](#), [T. Aaron Gulliver 2](#), [T. Aaron Gulliver 3](#),

[Xiang-dong Hou](#),

[W. Cary Huffman 1](#), [W. Cary Huffman 2](#), [W. Cary Huffman 3](#),

[Jennifer D. Key](#),

[Jon-Lark Kim 1](#), [Jon-Lark Kim 2](#),

[Mikhail Klin 1](#), [Mikhail Klin 2](#), [Mikhail Klin 3](#),

[Gretchen Matthews 1](#), [Gretchen Matthews 2](#), [Gretchen Matthews 3](#), [Gretchen Matthews](#)

[4](#),

[V. K. Meher](#)



## ALGEBRAIC COMBINATORICS AND APPLICATIONS

### Designs and Codes

April 3-10, 2005

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### Scientific Program

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#### Current list of keynote speakers:

- [E. O'Brien](#): Effective algorithmic approaches to the construction and classification of finite groups ([abstract](#))
- A. E. Brouwer: TBA
- [G. Butler](#): Combinatorial problems from genomics ([abstract](#))
- [C. Colbourn](#): Cover-free Families and Topology-Transparent Communication ([abstract](#))
- [J. Dinitz](#): Perfect and Uniform One-factorizations of the complete graph([abstract](#))
- J. Doyen: Constructing combinatorial structures with prescribed numbers of orbits ([abstract](#))
- [H-D. Gronau](#): Super-simple designs([abstract](#))
- [G.B. Khosrovshahi](#): On the recursive constructions of large sets of t-designs ([abstract](#))
- E. Konstantinova: Reconstruction of permutations from their erroneous pattern ([abstract](#))
- V. Levenshtein: Graph reconstruction from metric balls of all its vertices ([abstract](#))
- [S. Magliveras](#): Group theoretic methods in the construction of large sets of t-designs ([abstract](#))
- [R. Matheron](#): Translation planes of order 32 with non-trivial translation complement ([abstract](#))
- [P. Östergård](#): Classification of Combinatorial Designs ([abstract](#))
- [V. Pless](#): Binary Self-Dual Codes and Formally Self-Dual Codes ([abstract](#))
- [C. Praeger](#): On point-imprimitive, block-transitive designs ([abstract](#))
- [T. v. Tran](#): On Covering Arrays ([abstract](#))
- [W. Willems](#): Error probabilities in data transmissions ([abstract](#))
-

# Što je asocijacijska shema?

## Contributed Talks:

Each conference delegate is invited to present a contributed Talk. The time-limit for these talks will be 25 minutes.

- [R. F. Bailey](#): Permutation groups, Error-correcting Codes and Uncoverings ([abstract](#))
- [Y. Ben-Haim](#): Exact Minimum Density of Codes Identifying Vertices in the Square Grid ([abstract](#))
- [A. Betten](#): Geometric Codes and Hyperovals ([abstract](#))
- [M. Bogaerts](#): Permutation Arrays and Isometries of  $\text{Sym}(n)$  ([abstract](#))
- [N. Bougard](#): Lotto designs and Lotto numbers ([abstract](#))
- [M. Braun](#): Designs over finite fields ([abstract](#))
- [J. De Beule](#): The Hermitian variety  $H(5,4)$  has no ovoid ([abstract](#))
- [M. Buratti](#): Graph decompositions with a prescribed automorphism group ([abstract](#))
- [D. Cera](#):  $t$ -dependent sets in finite projective groups ([abstract](#))
- [A. Cossentin](#): Covers and partial spreads of polar spaces ([abstract](#))
- [M. Klin](#): Siamese association schemes and Siamese Steiner designs (45min) ([abstract](#))
- [A. Kohnert](#): Construction of optimal Codes ([abstract](#))
- [I. Kovacs](#): On Cayley digraphs of semidirect products of abelian groups ([abstract](#))
- [V. Krcadinac](#): Finite linear spaces consisting of two symmetric configurations ([abstract](#))
- [C.Y. Ku](#): Intersecting families of set partitions ([abstract](#))
- [P. Lisonek](#): Enumeration of codes of fixed cardinality up to isomorphism ([abstract](#))
- [S. Molodtsov](#): Computer construction of minimal graphs of diameter 2 ([abstract](#))
- [M. Muzychuk](#): New series of strongly regular graphs ([abstract](#))
- [D. Nikolova](#): Characterisation of Finite Soluble Groups by Two-Variable Commutator Identities ([abstract](#))

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- (2)  $T_0 = \{0\}$  and  $\bigcup_{i=0}^d T_i = H$ , that is  
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# Što je asocijacijska shema?

## Coherent configurations

A. E. Brouwer

### Abstract

Definition and a few examples.

### 0.1 Relations

A *coherent configuration* is a finite set  $X$  (of *points*) together with a collection  $\mathcal{R} = \{R_i \mid i \in I\}$  of nonempty binary relations on  $X$ , satisfying the following four conditions:

(i)  $\mathcal{R}$  is a partition of  $X \times X$ , that is, any ordered pair of points is in a unique relation  $R_i$ .

(ii) There is a subset  $H$  of the index set  $I$  such that  $\{R_h \mid h \in H\}$  is a partition of the diagonal  $\{(x, x) \mid x \in X\}$ .

(iii) For each  $R_i$ , its converse  $\{(y, x) \mid (x, y) \in R_i\}$  is also one of the relations in  $\mathcal{R}$ , say,  $R_{i'}$ .

(iv) For  $i, j, k \in I$  and  $(x, y) \in R_k$ , the number of  $z \in X$  such that  $(x, z) \in R_i$  and  $(z, y) \in R_j$  is a constant  $p_{ij}^k$  that does not depend on the choice of  $x, y$ .

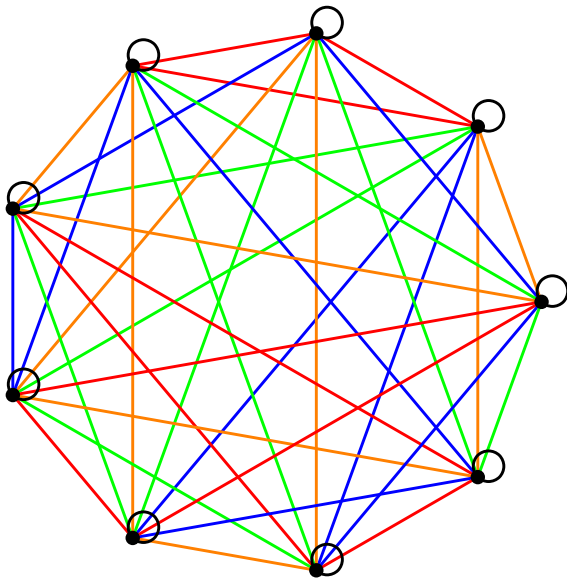
Coherent configurations were introduced by Higman in order to ‘do group theory without groups’, see example (ii) below.

The number  $|I|$  of relations is called the *rank* of the coherent configuration.

From (ii) we get a partition of  $X$  into sets  $X_h$  ( $h \in H$ ) called *fibers*, defined by  $R_h = \{(x, x) \mid x \in X_h\}$  for  $h \in H$ . It follows from (iv) that for any  $i \in I$  we have  $R_i \subseteq X_s \times X_t$  for certain fibers  $X_s, X_t$ . Consequently, any subset  $H_0$  of  $H$  determines a sub-cc with point set  $\bigcup_{h \in H_0} X_h$ .

# Što je asocijacijska shema?

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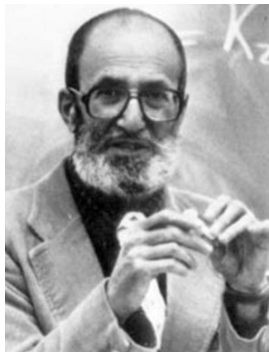


# Što je asocijacijska shema?

$$\begin{bmatrix} 0 & 1 & 1 & 2 & 2 & 3 & 3 & 4 & 4 \\ 1 & 0 & 1 & 3 & 4 & 2 & 4 & 2 & 3 \\ 1 & 1 & 0 & 4 & 3 & 4 & 2 & 3 & 2 \\ 2 & 3 & 4 & 0 & 3 & 2 & 1 & 1 & 4 \\ 2 & 4 & 3 & 3 & 0 & 1 & 2 & 4 & 1 \\ 3 & 2 & 4 & 2 & 1 & 0 & 4 & 3 & 1 \\ 3 & 4 & 2 & 1 & 2 & 4 & 0 & 1 & 3 \\ 4 & 2 & 3 & 1 & 4 & 3 & 1 & 0 & 2 \\ 4 & 3 & 2 & 4 & 1 & 1 & 3 & 2 & 0 \end{bmatrix}$$



# Što je asocijacijska shema?



A good stack of examples, as large as possible, is indispensable for a thorough understanding of any concept, and when I want to learn something new, I make it my first job to build one.

— *Paul Halmos* —

## Chris Godsil

### Introduction

I am a retired professor in [Combinatorics and Optimization](#) in the [Math Faculty](#) at the [University of Waterloo](#). The main purpose of these pages is to provide information about research in which I am involved, with my students and postdocs.

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[Algebraic Graph Theory](#). Our group's webpage. We run a weekly seminar in algebraic graph theory, more about this [here](#).

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### Other talks

1. [Notes](#) and [slides](#) for a talk "Quantum Colouring and Derangements".
  2. [slides](#) for talk "Problems on Continuous Quantum Walks".
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### My Research

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#### Quantum Walks

[to be updated]

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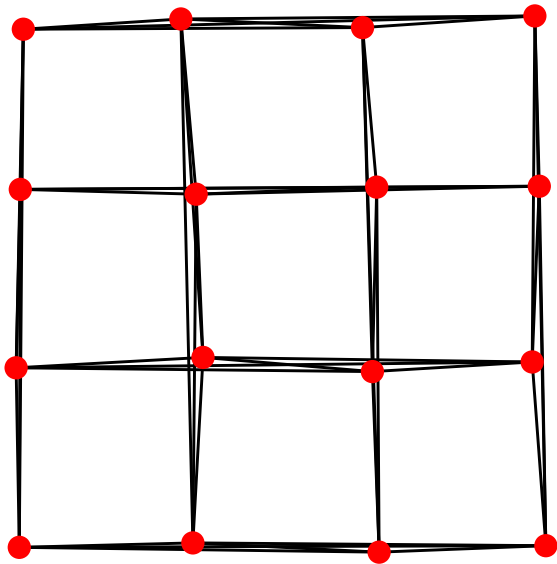
#### Covers

- [Contact](#)
- [Projects](#) - in algebraic graph theory.
- [Exercises in linear algebra](#).
- [Notes](#) - some published, some not
- [Advice](#) - mainly on writing and speaking
- [Talks](#)
- [My students](#) (and links to some theses)
- [Useful data, software](#)
- Preface to [Algebraic Combinatorics](#)
- [Algebraic Graph Theory](#) - co-authored with Gordon Royle
- [The Erdos-Ko-Rado Theorem: Algebraic Approaches](#) - co-authored with Karen Meagher, nothing here.
- [Discrete Quantum Walks on Graphs and Digraphs](#) - coauthored with Hanmeng Zhan
- [About Me](#)

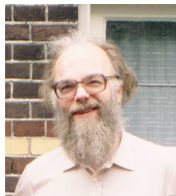
<https://www.math.uwaterloo.ca/~cgodsil/>

6. **Do not invent notation.**
7. Do not invent notation.
8. Well, you are only human, and you have this absolutely wonderful notational improvement, which must be released at once on an unsuspecting world. You should at least check that there is not a term already in use. If there is then you should use it instead. No one has ever gained even temporary fame in mathematics by introducing a new system of notation. You should also try to avoid the trap of believing that the notation used in your graduate school is the universal standard.
9. Cuteness is only tolerable in small children. This applies particularly to your choice of notation.

# Topovski graf



## Andries E. Brouwer



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[people at win.tue.nl](#) / [owinfo](#) / [library](#) / [ejw](#) / [eidma](#) / [diamant](#)

### Math

[List of \(mathematical\) publications](#) and available [preprints](#).

### Algebraic graph theory

A feeble attempt to make the files with [Additions and Corrections](#) to 'Distance-Regular Graphs' by Brouwer, Cohen and Neumaier (Springer, 1989) available. The source is some troff dialect, with most formatting commands removed. One further correction ([PDF](#)). Yet [another](#).

[Info](#) on email server (that stopped working mid 2004) with information on distance-regular graphs.

Machine-readable [intersection arrays](#) for distance-regular graphs.

[Spectra of graphs](#), extended course notes.

A [table of parameters of strongly regular graphs](#).

A [table of parameters of directed strongly regular graphs](#).

<https://www.win.tue.nl/~aeb/>

## Parameters of Strongly Regular Graphs

Below tables with parameters for strongly regular graphs.

The columns are:

- existence
- $v$  - number of vertices
- $k$  - valency
- $\lambda$  - number of common neighbours of two adjacent vertices
- $\mu$  - number of common neighbours of two nonadjacent vertices
- $r^f$  - positive eigenvalue with multiplicity
- $s^g$  - negative eigenvalue with multiplicity
- comments

The comments are undocumented at present. Ask.

[1-50 vertices](#)

[51-100 vertices](#)

[101-150 vertices](#)

[151-200 vertices](#)

[201-250 vertices](#)

<https://www.win.tue.nl/~aeb/graphs/srg/srgtab.html>

[Prev](#) [Up](#) [Next](#)

	v	k	$\lambda$	$\mu$	$r^f$	$s^g$	comments
!	5	2	0	1	$0.618^2$	$-1.618^2$	pentagon; Paley(5); Seidel 2-graph*
!	9	4	1	2	$1^4$	$-2^4$	Paley(9); $3^2$ ; 2-graph*
!	10	3	0	1	$1^5$	$-2^4$	<a href="#">Petersen</a> graph; $\text{NO}^-(4,2)$ ; $\text{NO}^{\text{-orth}}(3,5)$ ; switch $\text{OA}(3,2)^+*$ ; 2-graph
		6	3	4	$1^4$	$-2^5$	Triangular graph T(5); 2-graph
!	13	6	2	3	$1.303^6$	$-2.303^6$	Paley(13); 2-graph*
!	15	6	1	3	$1^9$	$-3^5$	$\text{O}(5,2)$ $\text{Sp}(4,2)$ ; $\text{NO}^-(4,3)$ ; $\text{GQ}(2,2)$ ; 2-graph*
		8	4	4	$2^5$	$-2^9$	Triangular graph T(6); 2-graph*
!	16	5	0	2	$1^{10}$	$-3^5$	$q222=0$ ; $\text{VO}^-(4,2)$ affine polar graph; projective binary [5,4] code with weights 2, 4; $\text{RSHCD}^-$ ; 2-graph
		10	6	6	$2^5$	$-2^{10}$	Clebsch graph; $q111=0$ ; from $2-(4,2,1)$ with 1-factor <a href="#">Fickus et al.</a> ; 2-graph
2!	16	6	2	2	$2^6$	$-2^9$	<a href="#">Shrikhande</a> graph; $4^2$ ; Wallis $(\text{AR}(2,1)+\text{S}(2,2,4))$ ; from a partial spread; projective binary [6,4] code with weights 2, 4; $\text{RSHCD}^+$ ; 2-graph
		9	4	6	$1^9$	$-3^6$	$\text{OA}(4,3)$ ; $\text{Bilin}_{2 \times 2}(2)$ ; Wallis2 $(\text{AR}(2,1)+\text{S}(2,2,4))$ ; Goethals-Seidel(2,3); $\text{VO}^+(4,2)$ affine polar graph; 2-graph
!	17	8	3	4	$1.562^8$	$-2.562^8$	Paley(17); 2-graph*
!	21	10	3	6	$1^{14}$	$-4^6$	
		10	5	4	$3^6$	$-2^{14}$	Triangular graph T(7)
-	21	10	4	5	$1.791^{10}$	$-2.791^{10}$	Conf
!	25	8	3	2	$3^8$	$-2^{16}$	$5^2$
		16	9	12	$1^{16}$	$-4^8$	$\text{OA}(5,4)$
15!	25	12	5	6	$2^{12}$	$-3^{12}$	<a href="#">Paulus</a> and <a href="#">Rozenfel'd</a> ; Paley(25); $\text{OA}(5,3)$ ; 2-graph*
10!	26	10	3	4	$2^{13}$	$-3^{12}$	<a href="#">Paulus</a> and <a href="#">Rozenfel'd</a> ; switch $\text{OA}(5,3)^+*$ ; 2-graph

<https://www.win.tue.nl/~aeb/graphs/srg/srgtab.html>


## Peter Cameron's homepage

Welcome to my new homepage on GitHub.  This page is under construction (and probably always will be!)

I am a quarter-time Professor in the School of Mathematics and Statistics at the University of St Andrews, and an Emeritus Professor of Mathematics at Queen Mary, University of London. In addition, I am an associate researcher at CEMAT, University of Lisbon, Portugal.

I am a Fellow of the [Royal Society of Edinburgh](#).

### About me

- [My official page](#)
- [My diary](#)
- [zbMATH profile](#), [MathSciNet profile](#), [Google Scholar](#)
- ORCID record:  [orcid.org/0000-0003-3130-9505](https://orcid.org/0000-0003-3130-9505)
- [Mathematical genealogy](#), [Wikipedia page](#)
- [CV and publications](#) (PDF)
- [Biographical stuff](#), [travel diaries](#)

### On this site

- [Talks](#), [publications](#), [conjectures](#), [coauthors](#), [students](#)
- Books: [Introduction to Algebra](#), [Combinatorics](#), [Notes on Counting](#), [Permutation Groups](#), [Sets, Logic and Categories](#) (some dead links to be sorted out)
- [Problems from my QMUL homepage](#)



### Elsewhere

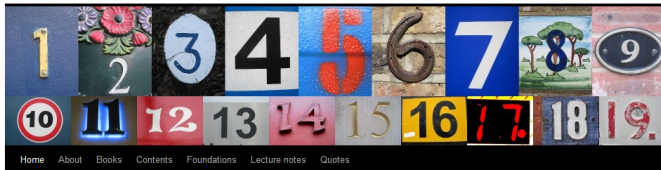
- [My homepage at QMUL](#)
- [Papers on arXiv](#)
- [Algebra and Combinatorics](#) at St Andrews
- [British Combinatorial Committee, BCC Conference List](#)
- [St Andrews pure mathematics seminars](#)
- [CIRCA](#)
- [ORCID](#)
- [Lecture notes](#)
- [Australasian Journal of Combinatorics](#)
- [Cameron Counts](#)
- [Mathematical quotes](#)
- [The Infinite Quest](#), a short course from the IAI Academy
- [Mathematics: the next generation](#) (LMS-Gresham lecture)

<https://cameroncounts.github.io/web/>



## Peter Cameron's Blog

*always busy counting, doubting every  
figured guess ...*



[Home](#) [About](#) [Books](#) [Contents](#) [Foundations](#) [Lecture notes](#) [Quotes](#)

### Ordering groups by element orders

Posted on 30/10/2023 by Peter Cameron

Recently a couple of people have asked me questions, or suggested research topics, related to what appear to be elementary properties of finite groups, but on examination, show unexpected complexities. Part of the reason why group theory is such an endlessly fascinating topic. This one comes from Hiranya Kishore Dey in Bangalore, India. I hope to discuss the other one soon.

The paper we wrote is on the arXiv, [2310.06516](https://arxiv.org/abs/2310.06516). So you can read it if you want. There is an elephant in the room, which I will talk about later. (I hope this is an acceptable metaphor for a paper with an Indian co-author.)

Let  $G$  be a finite group of order  $n$ . Its order sequence,  $os(G)$ , is the  $n$ -tuple of orders of the elements of  $G$ , arranged in non-decreasing order (so starting with 1 for the identity). The order sequences are partially ordered, where one sequence dominates another if every

#### Top Posts

- [Ordering groups by element orders](#)
- [Some challenges on Latin squares](#)
- [Mathematics and poetry](#)
- [Challenges in combinatorial design theory](#)
- [Mathematics and religion?](#)
- [Infinite reactions, 3](#)
- [Ian Macdonald](#)
- [The prehistory of the Higman-Sims graph](#)
- [Contents](#)
- [Fear of mathematics](#)

#### Recent comments

- [Peter Cameron on Challenges in combinatorial design theory](#)

<https://cameroncounts.wordpress.com/>

Strongly regular graphs stand on the cusp between the random and the highly structured. For example, there is (up to isomorphism) a unique  $\text{srg}(36, 10, 4, 2)$ ; but a computation by McKay and Spence [20] showed that the number of  $\text{srg}(36, 15, 6, 6)$ s is 32548. The pattern continues: there is a unique  $\text{srg}(m^2, 2(m-1), m-2, 2)$ , but more than exponentially many  $\text{srg}(m^2, 3(m-1), m, 6)$ s, as we will see.

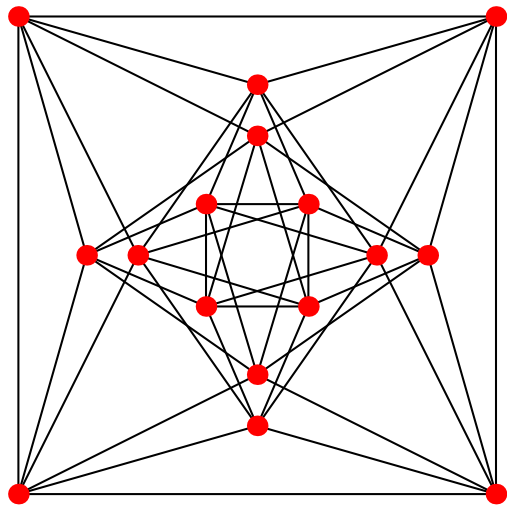
This suggests that no general asymptotic results are possible, and that, depending on the parameters, strongly regular graphs can behave in either a highly structured or an apparently random manner.

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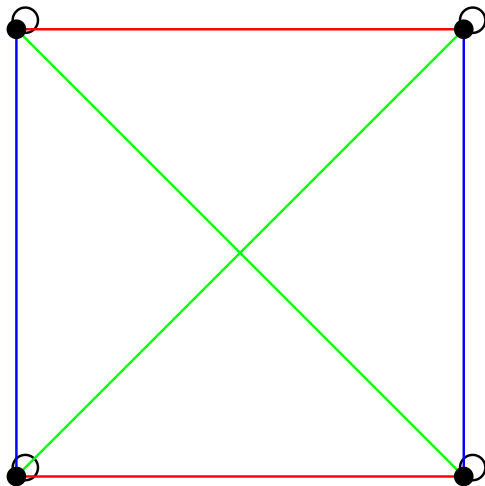
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<https://www.win.tue.nl/~aeb/graphs/srg/srgtab.html>

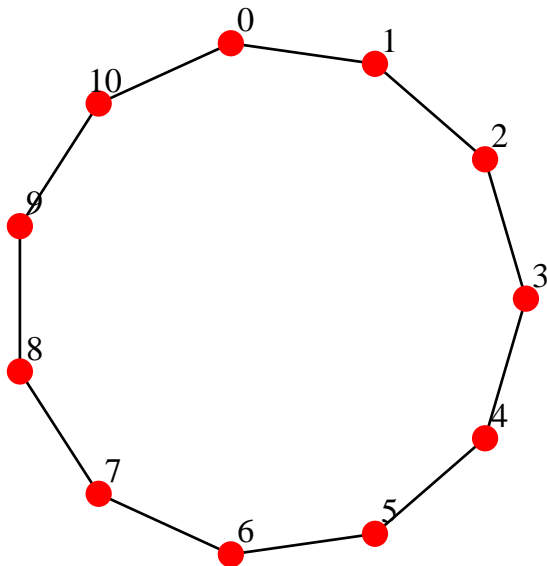
# Shrikhandeov graf



# Asocijacijska shema koja nije metrička



# Poligon reda $n = 11$



# Hiperkocka dimenzije $d = 4$ / Hammingova shema $H(4, 2)$

