Forkciphers: New and Exciting Symmetric Primitives

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Symmetric Primitives

Main Primitives

1. (Tweakable) block cipher: AES, Skinny, etc. (*T*)*PRP: Indistnguishabile from a random (tweakable) permutation*

2. Permutation: Keccak, PRIMATEs permutations, etc.

IP: Ideal permutation

3. Compression function: SHA2

Collision, second preimage and preimage resistance, PRF when keyed or ideal compression function



Use symmetric primitives in some composition to build provably secure cryptographic schemes processing arbitrary long inputs:

- Encryption schemes: CTR, CBC, etc.
- Message authentication codes: CBC-MAC, HMAC, PMAC, etc.
- Authenticated Encryption schemes: GCM, CCM, OCB, COLM, PRIMATEs, etc.

Question: Are we always using the right primitives for the right applications?

Authenticated Encryption

Data confidentiality and authentication

nonce-based AE(AD) syntax: a triplet $\Pi = (\mathcal{K}, Enc, Dec)$



inherent data expansion $|C| = |M| + \tau$

Authenticated Encryption of Short Messages

Efficiency for short messages

- ECRYPT-CSA Report, 2017: "The performance target is wrong ... Another increasingly common scenario is that an authenticated cipher is applied to many small messages ... The challenge here is to minimize overhead."
- NIST Requirements and Evaluation Criteria for LW Cryptography, May 24, 2018: AEAD submissions is that they shall be "optimized to be efficient for short messages (e.g., as short as 8 bytes)".

Numerous LW AEAD applications with short messages

- ✓ Automotive industry, e.g. CAN-FD automotive protocol payload≤ 64 bytes (4 blocks)
- ✓ 5G and LW communication protocols: Bluetooth, SigFox, LoraWan, and ZigBee protocols small status updates (one to few blocks)
- ✓ Narrowband IoT (NB-IoT) applications: smart sensors, traffic lights, smart parking, and smart <u>anything</u> 16 bits ≤ transport block size ≤ 680 bits
- $\checkmark\,$ Health applications
- \checkmark Industrial control systems

Yet, most AE schemes optimized for long messages!

|A| = a and |M| = m blocks

How many **extra** primitive calls to (a + m) for an AEAD?

	GCM	ССМ	OCB3	CLOC	TAE
Enc	m+1	m+1	m+1	т	<i>m</i> *
Auth	$a+m+1^{\#}$	a+m+1	a+1	a+m+1	$a^{*} + 1^{*}$
Extra	$1, m + 1^{\#}$	m + 2	2	m+1	1*

Nr of (BC, TBC^{*}, GF mul[#]) calls with m = |M| and a = |A|.

|A| = a and |M| = m blocks

How many **extra** primitive calls to (a + m) for an AEAD?

	GCM	ССМ	OCB3	CLOC	TAE
Enc	2	2	2	1	1*
Auth	2#	2	1	2	1*
Extra	$1,2^{\#}$	3	2	2	1*

Nr of (BC, TBC^{*}, GF mul[#]) calls with m = 1 and a = 0.

|A| = a and |M| = m blocks

How many **extra** primitive calls to (a + m) for an AEAD?

	GCM	CCM	OCB3	CLOC	TAE
Enc	2	2	2	1	1*
Auth	2#	2	1	2	1*
Extra	$1,2^{\#}$	3	2	2	1*

Nr of (BC, TBC^{*}, GF mul[#]) calls with m = 1 and a = 0.

Goal: achieve purely rate-1 **AE** scheme

A rate-1 AE makes (a + m) primitive calls to authenticate and encrypt (A, M).

At least 2 extra BC or 1 extra TBC primitive calls No expanding (inherent to AE) primitives



Question: Are we always using the right primitives for the right applications?

Existing primitives have no inherent AE security and structure

Forkcipher

Results in ^a and ^b

^aAndreeva et al. "ForkAE", second round candidate in the NIST LW Standardization Process, 2019 ^bAndreeva et al. "Forkcipher: A New Primitive for Authenticated Encryption of Very Short Messages", ASIACRYPT 2019

$$F: \mathcal{K} \times \mathcal{M} \times \mathcal{T} \mapsto \mathcal{C}_0 \times \mathcal{C}_1$$
 with $|\mathcal{M}| = |\mathcal{C}_0| = |\mathcal{C}_1|$





$$F: \mathcal{K} \times \mathcal{M} \times \mathcal{T} \mapsto \mathcal{C}_0 \times \mathcal{C}_1$$
 with $|\mathcal{M}| = |\mathcal{C}_0| = |\mathcal{C}_1|$

Output selection C_0



$$F: \mathcal{K} \times \mathcal{M} \times \mathcal{T} \mapsto \mathcal{C}_0 \times \mathcal{C}_1$$
 with $|\mathcal{M}| = |\mathcal{C}_0| = |\mathcal{C}_1|$

Output selection C_1



$$F: \mathcal{K} \times \mathcal{M} \times \mathcal{T} \mapsto \mathcal{C}_0 \times \mathcal{C}_1$$
 with $|\mathcal{M}| = |\mathcal{C}_0| = |\mathcal{C}_1|$

Inversion from either one or both C_0 and C_1



$$F: \mathcal{K} \times \mathcal{M} \times \mathcal{T} \mapsto \mathcal{C}_0 \times \mathcal{C}_1$$
 with $|\mathcal{M}| = |\mathcal{C}_0| = |\mathcal{C}_1|$





$$F: \mathcal{K} \times \mathcal{M} \times \mathcal{T} \mapsto \mathcal{C}_0 \times \mathcal{C}_1$$
 with $|\mathcal{M}| = |\mathcal{C}_0| = |\mathcal{C}_1|$

Reconstruction from C_1



$$F: \mathcal{K} imes \mathcal{M} imes \mathcal{T} \mapsto \mathcal{C}_0 imes \mathcal{C}_1$$
 with $|\mathcal{M}| = |\mathcal{C}_0| = |\mathcal{C}_1|$



Minimizes overhead

Under some *appropriate definition* forkcipher securely authenticates and encrypts *M*.

Forkcipher security



Pseudorandom forked permutation PRFP

Indistinguishability from a pair of random permutations under chosen ciphertext attack

$$\mathsf{Adv}^{\mathsf{prfp}}(\mathcal{D}) = \mathsf{Pr}[\mathcal{K} \leftarrow^{\$} \mathcal{K} : \mathcal{D}^{\mathsf{F}_{\mathcal{K}}} \Rightarrow 1] - \mathsf{Pr}[\mathcal{D}^{\pi_0, \pi_1} \Rightarrow 1].$$

iterate-fork-iterate (IFI) generic approach: allows reuse of iterative (T)BC structures



Primitive F	п	t	t + K
ForkSkinny-64-192	64	64	192
ForkSkinny-128-192	128	64	192
ForkSkinny-128-256	128	128	256
ForkSkinny-128-288	128	128	288

ForkSkinny



RF: round function; TKS: tweakey schedule; BC: branch constant; r_{init} , $r_0 = r_1$: nr rounds before and after fork.

Primitive	block	tweak	tweakey	r _{init}	r ₀	r_1
ForkSkinny-64-192	64	64	192	17	23	23
ForkSkinny-128-192	128	64	192	21	27	27
ForkSkinny-128-256	128	128	256	21	27	27
ForkSkinny-128-288	128	128	288	25	31	31

ForkSkinny cryptanalysis

- Inherits many of the SKINNY results
- Our cryptanalysis:
 - \checkmark truncated and impossible differential
 - ✓ boomerang
 - ✓ meet-in-the-middle
 - \checkmark integral and algebraic
- Forkcipher-specific:
 - \checkmark reconstruction attacks
 - $\checkmark\,$ branch constant and forking point
- Third party cryptanalysis by A. Bariant et al. at ToSC 2020: the best attacks on Skinny can be extended to 1 more round for most ForkSkinny variants, and at most 3 more rounds for ForkSkinny-128-256.

Question

Can we construct secure AEAD modes of rate-1?

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Yes

we design parallel **PAEF** and **rPAEF** and sequential **SAEF** rate-1 modes with ForkSkinny.

Parallel AE from a Forkcipher: PAEF



n-bit AE security

 $egin{aligned} & Adv_{PAEF}^{privacy}(\mathcal{A}) \leq Adv_{F}^{PRFP}(\mathcal{D}) \ \\ & Adv_{PAEF}^{auth}(\mathcal{A}) \leq Adv_{F}^{PRFP}(\mathcal{D}) + rac{q_v \cdot 2^n}{(2^n - 1)^2} \end{aligned}$

Reduced Parallel AE from a Forkcipher: rPAEF



$$\mathsf{Adv}_{\mathsf{rPAEF}}^{\mathsf{auth}}(\mathcal{A}) \leq \mathsf{Adv}_{\mathsf{F}}^{\mathsf{PRFP}}(\mathcal{D}) + rac{q_v \cdot 2^n}{(2^n-1)^2}$$

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Sequential AE from a Forkcipher: SAEF



n/2-bit AE security

$$egin{aligned} & Adv_{SAEF}^{privacy}(\mathcal{A}) \leq Adv_{F}^{PRFP}(\mathcal{D}) + 2rac{(\sigma-q)^2}{2^n} \ & Adv_{SAEF}^{auth}(\mathcal{A}) \leq Adv_{F}^{PRFP}(\mathcal{D}) + rac{2(\sigma-q+1)^2}{2^n} + rac{\sigma(\sigma-q)}{2^n} + rac{q_v(q+2)}{2^n} \ & 1 \end{aligned}$$

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Software implementation

Results in ^a and ^b

^ahttps://github.com/byt3bit/forkae

 $^{b}\mbox{A}.$ Deprez Master Thesis 2020, Optimized software implementations for ForkAE

Portable SW implementations

• Efficient and constant-time ForkAE SW implementations at https://github.com/rweather/lightweight-crypto

	Α	rm Cortex-	A9		Arm Cortex-M0				
	cycles/B	ROM (B)	RAM (B)	сус	les/B	ROM (E	B) RAM (E	B)	
PAEF-ForkSkinny-64-192	1669	3067	107	4	002	2067	107		
PAEF-ForkSkinny-128-192	1072	3187	161	2	457	2251	161		
PAEF-ForkSkinny-128-256	1074	3219	169	2	458	2247	169		
PAEF-ForkSkinny-128-288	1408	3483	189	3	408	2541	189		
SAEF-ForkSkinny-128-192	1075	3015	161	2	475	2187	161		
SAEF-ForkSkinny-128-256	1076	3043	169	2	476	2173	169		

- Decryption can further improved with preprocessed TKS https://github.com/ArneDeprez1/ForkAE-SW
 - \checkmark 38% less clock cycles
 - ✓ 1kB smaller ROM size
 - ✓ 252-696 bytes higher RAM usage

Table-based SW implementations

- Suitable for platforms without a cache, e.g. Cortex-M0
- Efficient implementations by combining different steps of the round function in XOR of table-lookups.

1 round = 18 lookups + 19 XOR

- SW performance on Arm Cortex-M0 compared to portable implementations:
 - ✓ Encryption: up to 20% faster
 - $\checkmark\,$ Decryption: up to 25% faster
 - $\checkmark\,$ Increased memory cost for storing 4 tables of 1kB each
 - ✓ Memory impact can be reduced by using only 1 table of 1kB without significant loss of performance
- https://github.com/ArneDeprez1/ForkAE-SW

Neon SIMD SW implementations

- Platforms with SIMD hardware extensions can exploit data-level parallelism in ForkSkinny primitive
 - $\checkmark\,$ RF-parallelism: S-box in parallel for every cell
 - $\checkmark\,$ Fork parallelism: compute 2 branches parallel
- Implementation for Neon SIMD on Arm Cortex-A9 https://github.com/ArneDeprez1/ForkAE-SW
- 128-bit instances (S-box parallelism) :
 - ✓ 30% less clock cycles
 - $\checkmark~$ 0.5 kB reduction in ROM size
 - ✓ RAM size equal
- 64-bit instance (S-box + fork parallelism):
 - \checkmark 29 % less clock cycles
 - ✓ ROM size approx. equal
 - ✓ RAM size increased

Hardware implementation

Results in ^a and ^b

^aT. Purnal et al. "What the Fork: Implementation Aspects of Forkcipher", NIST LW Workshop 2019 ^bJ. Pittevils Master Thesis 2020, "Low-area Optimized Hardware Implementations for ForkAE"

HW comparison ¹

Implementation	Area [GE]	Area [CE]	Number of cycles for encrypting $(a + m)$ 64-bit blocks						
(round based)	F ONLY		a = 0			a = 1			Conoral
(Tound=based)	E-ONLI	LINCIDEC	m = 1	m = 2	<i>m</i> = 3	m = 0	m = 1	m = 2	General
Sk-AEAD M6	8095	9458	96	96	144	48	96	96	$48\left(\left\lceil \frac{a}{2}\right\rceil + \left\lceil \frac{m}{2}\right\rceil + 1\right)$
PAEF-64-192	5034	6704	63	126	189	40	103	166	40(a + 1.575m)
PAEF-64-192 (//)	5500	7422	40	80	120	40	80	120	40(a + m)

Implementation	Area [GE]	Area [CE]	Number of cycles for encrypting $(a + m)$ 128-bit blocks						
(round based)	E ONIX	EvoDpo		<i>a</i> = 0			a = 1		Conorol
(Tound-based)	E-ONLI	LINCIDEC	m = 1	m = 2	<i>m</i> = 3	m = 0	m = 1	m = 2	General
Romulus-N3	6288	6406	96	144	192	48	96	144	$48(\lceil \frac{a-1}{1.75}\rceil + m + 1)$
SAEF-128-192	7197	9203	75	150	225	48	123	198	48(a + 1.562m)
SAEF-128-256	7740	9999	75	150	225	48	123	198	48(a + 1.562m)
SAEF-128-192 (//)	7713	10804	48	96	144	48	96	144	48(a + m)
SAEF-128-256 (//)	8288	11646	48	96	144	48	96	144	48(<i>a</i> + <i>m</i>)
SK-AEAD M5	8746	10109	96	144	192	96	144	192	48(a + m + 1)
PAEF-128-192 (//)	8020	11112	48	96	144	48	96	144	48(a+m)
PAEF-128-256 (//)	8745	12103	48	96	144	48	96	144	48(a+m)
rPAEF (aggr.) (//)	8203	na	87	135	183	48	135	183	48(a+m) + 39
Romulus-N1	7018	7136	112	168	224	56	112	168	$56\left(\left\lceil \frac{a-1}{2}\right\rceil + m + 1\right)$
Sk-AEAD M1-2	9966	12363	112	168	224	112	168	224	56(a + m + 1)
PAEF-128-288	9274	11705	87	174	261	56	143	230	56(a + 1.553m)
PAEF-128-288 (//)	10141	13697	56	112	168	56	112	168	56(a + m)
rPAEF (const.) (//)	8178	na	87	143	199	56	143	199	56(a+m)+31

(//) ForkSkinny-level parallelism; (SFF/MUX/XOR/NAND with 7.67/2.33/2/1 GE)

 $^1\mathrm{T.}$ Purnal et al. "What the Fork: Implementation Aspects of Forkcipher", NIST LW Workshop 2019



Speed-area exploration (64 bits)



Speed-area exploration (128 bits)



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Low-area ForkSkinny HW architectures²



 $^{^2\,^{\}prime\prime}\text{Low-area}$ Optimized Hardware Implementations for ForkAE" Master Thesis 2020 by Jowan Pittevils

Word-based architectures results

Algorithm	Architocturo	Area [GE]	Area [GE]	Delay [ns]	Cycles	T'put enc [kbit/s]	T'put dec [kbit/s]
Aigontinin	Architecture	E-only	EncDec			E-only	EncDec
Skinny-64-192		2448	3754	1.04	872	7.33	3.7
Skinny-128-256		3525	5499	0.94	1040	12.29	6.2
Skinny-128-384		4680	7157	0.93	1208	10.58	5.4
ForkSkinny-64-192	Restart	2718	na	1.15	2218	2.8-5.7	na
ForkSkinny-128-256	Restart	3917	na	1.19	2638	4.8-9.7	na
ForkSkinny-128-288	Restart	4567	na	1.39	3058	4.2-8.4	na
ForkSkinny-64-192	Retrace	3867	3894	1.67	2328	2.7-5.5	2.3- 4.6
ForkSkinny-128-256	Retrace	5648	5685	1.73	2748	4.7-9.3	3.9- 7.8
ForkSkinny-128-288	Retrace	6645	6650	1.92	3168	4.0-8.1	3.3- 6.7
ForkSkinny-64-192	ForkReg	3243	4470	0.93	1362	4.7- 9.3	2.3- 4.6
ForkSkinny-128-256	ForkReg	4977	6787	1.4	1614	7.9- 15.9	3.9- 7.8
ForkSkinny-128-288	ForkReg	5629	7795	1.23	1866	6.8- 13.7	3.3- 6.7

(SFF/MUX/XOR/NAND with 7.67/2.33/2/1 GE)

- ForkSkinny area very close to Skinny for enc.only (Restart)
- ForkSkinny area-usage very close to Skinny for enc./dec. (Retrace)
- Serial ForkSkinny better throughput than serial Skinny for short messages, both for enc.only (Forkreg) and enc./dec. (Retrace)

Our ForkAE Design

Secure

- \checkmark Well-analysed: based on $\rm Skinny$
- ✓ Provably secure: PAEF, rPAEF, SAEF

Efficient

- ✓ Excellent performance for small messages
- \checkmark Excellent throughput per area in HW
- $\checkmark\,$ Inherits LW implementation features of $_{\rm SKINNY}$
- $\checkmark\,$ Multiple trade-offs in speed-resource design space

Flexible

key size: 128 bits and variable block, nonce, tag sizes

Generalization: Multi-Forkcipher

Multi-Forkcipher with s = 3



Forward algorithm

$$MFC_s: \mathcal{K} \times \mathcal{T} \times \mathcal{M} \times 2^{\{1,2,\dots,s\}} \rightarrow \bigcup_{e=1}^s \{0,1\}^{en}$$

and the backward (or the inversion) algorithm

$$MFC_s^{-1}: \mathcal{K} \times \mathcal{T} \times \mathcal{C} \times \{1, 2, \dots, s\} \times 2^{\{i, 1, 2, \dots, s\}} \rightarrow \bigcup_{e=1}^s \{0, 1\}^{en}$$

- When s = 1, then MFC = TBC
- When s = 2, then MFC = FC

MFC security



Pseudorandom multi-fork permutation

Indistinguishability from *s*-tuple of independent random permutations

$$\mathsf{Adv}^{\mathsf{prtmfp}}(\mathcal{D}) = \mathsf{Pr}[\mathcal{K} \leftarrow^{\$} \mathcal{K} : \mathcal{D}^{\mathsf{MFC}^s_{\mathcal{K}}} \Rightarrow 1] - \mathsf{Pr}[\mathcal{D}^{\pi_1, \dots, \pi_s} \Rightarrow 1].$$

- MFC with authenticated encryption MFC-AE brings in benefits for even longer messages, i.e. depending on the input message, adjustments possible to number of branches needed.
- Replace a TBC with MFC = allows for larger pseudorandom string output generation with strong security benefits.

Question: where can we effectively replace TBC with an MFC and gain in efficiency?

Multi-forkciphers for Encryption^a

^ajoint work with A. Singh Bhati, B. Preneel, and D. Vizár

Study the security and efficiency of MFCs in a CTR-style mode motivated by:

- MFC uses in forward-only direction
- Possibility to obtain BBB security and/or graceful security degradation with nonce repetitions (like CTRT: CounTeR in Tweak [Peyrin and Seurin'15])
- Systematic investigation of tweakable CTR variants with random *IV* and/or nonce *N*
- Provide security/efficiency analysis of CTR-style mode variants with MFC

Tweakable CTR framework

Tweakable CTR framework

• Tweakable CTR (TCTR) takes a *sequence* of **tweak-input** pairs, and generates key stream by applying a MFC to each pair.



• X_i-s and T_i-s generated with N and/or a random IV and/or a counter.

Generic CTR Encryption Mode

Generic CTR Encryption Mode

GCTR is defined via TCTR_s



- $f_X(N, R, j)$ and $f_T(N, R, j)$ are input-tweak (X_j, T_j) generating functions
- exhaustive study of all f_X and f_T with $\{\parallel, \oplus, \operatorname{copy}\}$
- varying security (BB, BBB, NMR, NAE)
- usage constraints (tradeoff of the size of the parameters)
- example: counter in tweak CTRT has $X_j = N$ and $T_j = R \oplus j$

Security Model: Nonce and IV-based Encryption (nivE)

- An nivE scheme $\Pi = (\mathcal{K}, \mathcal{E}, \mathcal{D})$ with $\mathcal{E} : \mathcal{K} \times \mathcal{N} \times \mathcal{R} \times \mathcal{M} \to \{0, 1\}^*$ and $\mathcal{D} : \mathcal{K} \times \mathcal{N} \times \mathcal{R} \times \{0, 1\}^* \to \mathcal{M}$
- Let *E*^{\$} : *K* × *N* × *M* → *R* × {0,1}* denote the randomized encryption algorithm, which internally samples an *R* ←^{\$} *R*, computes *C* ← *E*(*K*, *N*, *R*, *M*) and returns *R*, *C*. We further let *E*^{\$}_K(*N*, *M*) = *E*^{\$}(*K*, *N*, *M*).

nivE indistinguishability of ciphertexts from random strings in a chosen plaintext attack for a nonce respecting adversary A is defined as:

$$Adv_{\Pi}^{nivE} = \left| \mathsf{Pr}\left[\mathcal{K} \leftarrow^{\$} \mathcal{K} : \mathcal{A}^{\mathcal{E}^{\$}_{\mathcal{K}}(\cdot, \cdot)} \Rightarrow 1 \right] - \mathsf{Pr}\left[\mathcal{A}^{\mathsf{Rand}^{\$}(\cdot, \cdot)} \Rightarrow 1 \right] \right|$$

The cost to compute 1 keystream *n*-bit block:

with ForkSkinny GCTR: 0.8 of cost with SKINNY GCTR

The cost to compute 1 keystream *n*-bit block:

with ForkSkinny GCTR: 0.8 of cost with SKINNY GCTR

ForkSkinny GCTR becomes **twice** faster than SKINNY GCTR using primitive level parallelism [NIST workshop'19] This work:

- New ForkSkinny forkcipher primitive
- New (multi-)forkcipher formalism (M)FTPRP
- ForkSkinny cryptanalysis
- New (multi-)forkcipher modes and proofs

Future work:

- New multi-forkcipher instantiations
- New multi-forkcipher paradigms
- Multi-forkcipher applications beyond AE and encryption
- Multi-forkcipher side-channel, quantum attacks, etc. resistance

https://github.com/byt3bit/forkae/



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Thank you!



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