

Teme i pojmovi za usmeni dio ispita iz Uvoda u algebarsku teoriju brojeva prema J.S.Milne: Algebraic Number Theory.

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4. Finding the ring of integers: Proposition 2.33.
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6. Dedekind's domains: page 38, Theorem 3.6.
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8. Factorization in extensions: Theorems 3.36, 3.37.
9. Finding factorizations: Theorem 3.43.
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Prema J.S.Milne: Fields and Galois theory.

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Zadaci koji se trebaju izraditi u MATEMATICI ili MAPLE-u.

1. Faktorizirajte $f(X) = 6X^2 + 18X - 24$ nad:
 - a) poljem racionalnih brojeva
 - b) $F_7[X]$
 - c) $F_{11}[X]$.
2. Faktorizirajte $f(X) = X^4 + 4$ nad:
 - a) poljem racionalnih brojeva
 - b) poljem generiranim korijenom polinoma $X^2 + 2X + 2$ nad \mathbf{Q} .
3. Odredite diskriminantu polinoma:
 - a) $f(X) = X^3 - 3X + 1$
 - b) $f(X) = X^3 + 3X + 1$
 - c) $f(X) = X^4 + 4X^2 + 2$
 - d) $f(X) = X^3 + aX^2 + bX + c$.
4. Odredite Galoisovu grupu polinoma iz zad. 3.
5. Odredite rastav ideala (2), (3) i (5) u $\mathbf{Q}[\alpha]$ ako je α korijen polinoma $f(X) = X^3 + 10X + 1$.
6. Odredite prvih 15 ciklotomskih polinoma.
7. Odredite fundamentalnu jedinicu realnog kvadratnog polja kojemu je diskriminanta redom: 5,8,12,13,17.